Fiscal Stimulus in a Monetary Union:
Evidence from U.S. Regions

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Abstract

We use rich historical data on military procurement spending across U.S. regions to estimate the effects of government spending in a monetary union. Aggregate military build-ups and draw-downs have differential effects across regions. We use this variation to estimate an “open economy relative multiplier” of approximately 1.5. We develop a framework for interpreting this estimate and relating it to estimates of the standard closed economy aggregate multiplier. The closed economy aggregate multiplier is highly sensitive to how strongly aggregate monetary and tax policy “leans against the wind.” In contrast, our open economy relative multiplier “differences out” these effects because different regions in the union share a common monetary and tax policy. Our estimates provide evidence in favor of models in which demand shocks can have large effects on output.

Keywords: Fiscal stimulus, Government Spending, Multiplier, Monetary Union.

JEL Classification: E62, E32

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1 Introduction

The effect of government spending on output is often summarized by a multiplier—the percentage increase in output that results when government spending is increased by 1 percent of GDP. There is a wide range of views about this statistic in the literature. On the one hand, the recent American Recovery and Reinvestment Act (ARRA)—perhaps the largest fiscal stimulus plan in U.S. history—was motivated by a relatively high estimate of the multiplier of 1.6 (Romer and Bernstein, 2009). Other studies argue that the multiplier is substantially smaller and potentially close to zero. In particular, if the determination of output is dominated by supply-side factors, an increase in government purchases to a large extent “crowds out” private sector consumption and investment.

The wide range of views on the multiplier arises in part from the difficulty of measuring it. Changes in government spending are rarely exogenous, leading to a range of estimates depending on the estimation approach.1 Two main approaches have been used to estimate the multiplier in the academic literature. The first is to study the output effects of increases in military spending associated with wars, which are plausibly unrelated to prevailing macroeconomic conditions (Ramey and Shapiro, 1998; Edelberg, Eichenbaum and Fisher, 1999; Burnside, Eichenbaum and Fisher, 2004; Ramey, 2011; Barro and Redlick, 2011; Fisher and Peters, 2010). This approach faces the challenge that large wars are relatively infrequent. Another challenge is confounding variation associated with tax increases, price controls, patriotism, and other macroeconomic shocks.2 The second main approach used to identify the multiplier is the structural VAR approach (Blanchard and Perotti, 2002; Perotti, 2007; Mountford and Uhlig, 2008; Ilzetzki, Mendoza and Vegh, 2013). This approach relies on structural assumptions about output and fiscal policy dynamics to estimate the multiplier.

The wide range of views on the multiplier also arises from contrasting results in the theoretical literature. The government spending multiplier is not a deep structural parameter like the elasticity of labor supply or the intertemporal elasticity of substitution. Different models, therefore, differ in their implications about the multiplier depending on what is assumed about preferences, technology, government policy and various “frictions.” Simple versions of the Neoclassical model generally imply a small multiplier, typically smaller than 0.5 (see, e.g., Baxter and King, 1993). The multiplier is sensitive to how the spending is financed—smaller if it is financed by distortionary taxes than lump

1For surveys of the existing evidence, see for example Perotti (2007), Hall (2009), Alesina and Ardagna (2009) and Cogan et al. (2010).

2Most of the evidence from this approach derives from the U.S. experience during WWII and the Korean War, when changes in U.S. military spending were largest and most abrupt as a fraction of total output. Hall (2009) and Barro and Redlick (2011) emphasize that it is not possible to draw meaningful inference using aggregate data on military spending after 1955 because there is insufficient variation in military spending in this period.
sum taxes.\textsuperscript{3} In New Keynesian models, the size of the multiplier depends critically on the extent to which monetary policy “leans against the wind.” Strongly counter-cyclical monetary policy—such as that commonly estimated for the Volcker-Greenspan period—can generate quite low multipliers—comparable to those for the Neoclassical model. However, when monetary policy is less responsive—e.g., at the zero lower bound—the multiplier can exceed two.\textsuperscript{4} Clearly, there is no “single” government spending multiplier. This is likely one contributing factor for the wide range of empirical estimates of the multiplier discussed above, since different identification schemes implicitly put different weight on periods when different policy regimes were in place.

We analyze the effects of government spending in a monetary and fiscal union—the United States. We estimate the effect that an increase in government spending in one region of the union relative to another has on relative output and employment. We refer to this as the “open economy relative multiplier.” We use variation in regional military procurement associated with aggregate military build-ups and draw-downs to estimate these effects.

The “open economy relative multiplier” we estimate differs conceptually from the more familiar “closed economy aggregate multiplier” that one might estimate using aggregate U.S. data. At first glance, this might seem to be a pure disadvantage, since much interest is focused on the closed economy aggregate multiplier. We show, however, that the open economy relative multiplier has important advantages. These advantages stem from the fact that relative policy is precisely pinned down across regions in the United States: The Federal Reserve cannot raise interest rates in some states relative to others, and federal tax policy is common across states in the union. We show that this property makes the open economy relative multiplier a powerful diagnostic tool for distinguishing among competing macroeconomic models.

Military spending is notoriously political and thus likely to be endogenous to regional economic conditions (see, e.g., Mintz, 1992). We, therefore, use an instrumental variables approach to estimate the open economy relative multiplier. Our instruments are based on two characteristics of military spending. First, national military spending is dominated by geopolitical events. Second, when national military spending rises by 1 percentage point of GDP, it rises on average by more than 3 percentage points in states that receive a disproportionate amount of military spending—such as California and Connecticut—but by less than one-half of one percent in states that don’t—such as


\textsuperscript{4}At the zero lower bound, fiscal stimulus lowers real interest rates by raising inflation (Eggertsson, 2010; Christiano, Eichenbaum, and Rebelo, 2011).
Illinois. We use this heterogeneity in the response of regional spending to national military buildups and draw-downs to identify the effects of government spending on output.\textsuperscript{5} Our identifying assumption is that the U.S. does not embark on military buildups—such as those associated with the Vietnam War and the Soviet invasion of Afghanistan—because states that receive a disproportionate amount of military spending are doing poorly relative to other states. This assumption is similar—but weaker than—the common identifying assumption in the empirical literature on the effects of national military spending, that variation in national military spending is exogenous to the U.S. business cycle. By including time fixed effects, we control for aggregate shocks and policy that affect all states at a particular point in time—such as changes in distortionary taxes and aggregate monetary policy.

We estimate the open economy relative multiplier to be roughly 1.5. In other words, when relative per-capita government purchases in a region rises by 1 percent of regional output, relative per-capita output in that region rises by roughly 1.5 percent. We develop a theoretical framework to help us interpret our estimate of the open economy relative multiplier and assess how it relates to the closed economy aggregate multiplier for the United States. Using this framework, we show that our estimate for the open economy relative multiplier favors models in which demand shocks can have large effects on output. Our estimates line up well with the open economy relative multiplier implied by an open economy New Keynesian model in which consumption and labor are complements.\textsuperscript{6} This model generates a large closed economy aggregate multiplier when monetary policy is unresponsive, such as when the nominal interest rate is at its zero lower bound. The “plain-vanilla” Neoclassical model, however, yields a substantially lower open economy relative multiplier, regardless of the monetary response.

The relative monetary policy across regions—fixed relative nominal rate and exchange rate—is more accommodative than “normal” monetary policy in the U.S.—which raises the real interest rate substantially in response to inflationary shocks such as government spending shocks. Our open economy relative multiplier is thus akin to a closed economy aggregate multiplier for a more accommodative monetary policy than the one seen in the U.S. under Volcker and Greenspan. This implies that our estimate of 1.5 for the open economy relative multiplier is perfectly consistent with

\textsuperscript{5}Since regional variation in military procurement is much larger than aggregate variation, this approach allows us to overturn the conclusion from the literature that focuses on aggregate data that little can be learned about fiscal multipliers from the post-1960 data. Data from this period has the advantage that it is less affected by unusual factors such as price controls, rationing, patriotism and large changes in taxes than data from the WWII and Korean War experiences (Perotti, 2007).

\textsuperscript{6}Another potential approach to matching our multiplier estimate would be to consider a model with “hand-to-mouth” consumers as in Gali, Lopez-Salido, and Valles (2007).
much lower existing estimates of the closed economy aggregate multiplier (e.g., those of Barro and Redlick, 2011).

Since the nominal interest rate is fixed across regions in our setting, one might think that our open economy relative multiplier would be akin to the closed economy aggregate multiplier when nominal interest rates are fixed at the zero lower bound, in which case the New Keynesian model generates large multipliers (Eggertsson, 2010; Christiano, Eichenbaum and Rebelo, 2011). We show that this is not the case. This simple intuition ignores a crucial dynamic aspect of price responses in a monetary union. Since transitory demand shocks do not lead to permanent changes in relative prices across regions and the exchange rate is fixed within the monetary union, any increase in prices in the short run in one region relative to the other must eventually be reversed in the long run. This implies that even though relative short-term real interest rates fall in response to government spending shocks in our model, relative long-term real interest rates don’t (in contrast to the zero lower bound setting). It is the fall in long-term real interest rates that generates a high multiplier in the zero lower bound setting. The absence of such a fall in our setting explains why the open economy relative multiplier generated by the baseline New Keynesian model is much lower than the closed economy aggregate multiplier at the zero lower bound.

The intuition for why the open economy relative multiplier is larger than the closed economy aggregate multiplier for normal monetary policy is similar to the intuition for why the government spending multiplier is larger under a fixed than a flexible exchange rate in the Mundell-Fleming model. In fact, we show that the open economy relative multiplier is exactly the same as the aggregate multiplier in a small open economy with a fixed exchange rate. Our estimate can, therefore, be compared with other estimates of multipliers in open economies with fixed exchange rates. Based on data from 44 countries, Ilzetzki, Mendoza, and Vegh (2013) estimate a multiplier of 1.5 for countries that operate a fixed exchange rate regime, but a much lower multiplier for countries operating a flexible exchange rate regime.7

An important difference between our open economy relative multiplier and the closed economy aggregate multiplier is that the regions that receive spending don’t have to pay for it. Could this perhaps explain the “large” relative multiplier we estimate? In this respect, it is important to keep in mind that in a Neoclassical model, an increase in wealth shifts labor supply in and thus reduces the multiplier. With sticky prices and home bias, an increase in wealth also increases aggregate demand for home goods, which acts to increase the multiplier. In our baseline model, we assume

7Kraay (2012) estimates a government spending multiplier of about 0.5 for 29 aid-dependent developing countries using variation in World Bank lending.
that financial markets are complete across regions. Thus any increase in wealth associated with the
government spending is fully shared with the rest of the economy. Following Farhi and Werning
(2012), we consider a version of our model in which financial markets are incomplete across regions.
We use this model to compare the effects of federally financed government spending and locally
financed government spending. For our baseline parameters, the open economy relative multiplier is
only slightly larger for federally financed spending than locally financed spending.

The theoretical framework we describe helps to interpret recent and ongoing research on the
effects of other forms of local government spending (Acconcia et al., 2011; Chodorow-Reich et al.,
2012; Clemens and Miran, 2012; Cohen et al., 2011; Fishback and Kachanovskaya, 2010; Serrato
and Wingender, 2010; Shoag, 2010; Wilson, 2011). In general, these studies appear to estimate open
economy relative multipliers of a similar magnitude as we do. There are, however, a few potentially
important differences between our study and these. Some of these studies focus on windfall transfers
rather than purchases. One advantage of our focus on military purchases is that it seems reasonable
to assume that they are separable from other forms of consumption, as is typically assumed in
macroeconomic models.

Our empirical approach builds on previous work by Davis, Loungani, and Mahidhara (1997), who
study several drivers of regional economic fluctuations, including military procurement. Several
other studies on the impact of regional defense spending are surveyed in Braddon (1995). The most
important difference in our empirical methodology relative to these studies is our use of variation
in aggregate military spending in creating instruments to account for potential endogeneity of local
procurement spending as well as measurement error. Our work is also related to Canova and Pappa
(2007), who study the price effects of fiscal shocks in a monetary union. Our theoretical analysis is
related to earlier work on monetary and fiscal policy in a monetary union by Benigno and Benigno

The remainder of the paper is organized as follows. Section 2 described the data we use. Section
3 presents our empirical results. Section 4 presents the model we use to interpret these empirical
results. Section 5 presents our theoretical results. Section 6 concludes.

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8Our open economy relative multiplier is not a “windfall” or “manna from heaven” multiplier. Rather, the spending
we study is akin to a foreign demand shock. Agents are getting paid to produce goods that are “exported” for use in
defense of the union as a whole.

9Similarly, Hooker and Knetter (1997) estimate the effects of military procurement on subsequent employment
growth using a somewhat different specification.
Data

Relative to other forms of federal government spending, the geographical distribution of military spending is remarkably well documented, perhaps because of the intense political scrutiny surrounding these purchases. Our main source for military spending data is the electronic database of DD-350 military procurement forms available from the US Department of Defense. These forms document military purchases of everything from repairs of military facilities to the purchase of aircraft carriers. They cover purchases greater than $10,000 up to 1983 and greater than $25,000 thereafter.\footnote{Purchases reported on DD-350 forms account for 90 percent of military purchases. DD-1057 forms are used to summarize smaller transactions but do not give the identity of individual sellers. Our analysis of census shipment data in section 3 suggests DD-350 purchases account for almost all of the time-series variation in total military procurement.} These data are for the federal government fiscal year.\footnote{Since 1976, this has been from October 1st to September 30th. Prior to 1976, it was from July 1st to June 30th.} We have used the DD-350 database to compile data on total military procurement by state and year for 1966-2006.\footnote{The electronic military prime contract data file was created in the mid-1960’s and records individual military prime contracts since 1966. This occurred around the time Robert McNamara was making sweeping changes to the procurement process of the U.S. Department of Defense. Aggregate statistics before this point do not appear to be a reliable source of information on military purchases since large discrepancies arise between actual outlays and procurement for the earlier period, particularly at the time of the Korean War. See the Department of Defense Greenbook for aggregate historical series of procurement and outlays.}

The DD-350 forms list prime contractors and provide information on the location where the majority of the work was performed. An important concern is the extent of inter-state subcontracting. To help assess the extent of such subcontracting, we have compiled a new dataset on shipments to the government from defense oriented industries. The source of these data are the Annual Survey of Shipments by Defense-Oriented Industries conducted by the US Census Bureau from 1963 through 1983. In section 3.2, we compare variation in procurement spending with these shipments data.

Our primary measure of state output is the GDP by state measure constructed by the U.S. Bureau of Economic Analysis (BEA), which is available since 1963. We also make use of analogous data by major SIC/NAICS grouping.\footnote{The data are organized by SIC code before 1997 and NAICS code after 1997. BEA publishes the data for both systems in 1997, allowing the growth rate series to be smoothly pasted together.} We use the Bureau of Labor Statistics (BLS) payroll survey from the Current Employment Statistics (CES) program to measure state-level employment. We also present results for the BEA measure of state employment which is available since 1969. We obtain state population data from the Census Bureau.\footnote{Between census years, population is estimated using a variety of administrative data sources including birth and death records, IRS data, Medicare data and data from the Department of Defense. Since 1970, we are also able to obtain population by age group, which allows us to construct estimates of the working age population.}

Finally, to analyze price effects, we construct state and regional inflation measures from several sources. Before 1995, we rely on state-level inflation series constructed by Marco Del Negro (1998)
for the period 1969-1995 using a combination of BLS regional inflation data and cost of living
estimates from the American Chamber of Commerce Realtors Association (ACCRA). After 1995, we
construct state-level price indexes by multiplying a population-weighted average of cost of living
indexes from the American Chamber of Commerce Realtors Association (ACCRA) for each region
with the US aggregate Consumer Price Index. Reliable annual consumption data are unfortunately
not available at the state level for most of the time period or regions we consider.

3 Measurement of the Open Economy Relative Multiplier

3.1 Empirical Specification and Identification

We use variation in military procurement spending across states and regions to identify the effects
of government spending on output. Our empirical specification is

\[
\frac{Y_{it} - Y_{it-2}}{Y_{it-2}} = \alpha_i + \gamma_t + \beta \frac{G_{it} - G_{it-2}}{Y_{it-2}} + \epsilon_{it},
\]

where \(Y_{it}\) is per-capita output in region \(i\) in year \(t\), \(G_{it}\) is per-capita military procurement spending in
region \(i\) in year \(t\), and \(\alpha_i\) and \(\gamma_t\) represent state and year fixed effects. The inclusion of state fixed
effects implies that we are allowing for state specific time trends in output and military procurement
spending. The inclusion of time fixed effects allows us to control for aggregate shocks and aggregate
policy—such as changes in distortionary taxes and aggregate monetary policy. All variables in the
regression are measured in per capita terms. We regress two-year changes in output on two-year
changes in spending, as a crude way of capturing dynamics in the relationship between government
spending and output. We use annual panel data on state and regional output and spending for

\(\text{See Appendix A of Del Negro (1998) for the details of this procedure.}\)

\(\text{Retail sales estimates from Sales and Marketing Management Survey of Buying Power have sometimes been used as a}
\text{proxy for state-level annual consumption. However, these data are constructed by using employment data to impute}
\text{retail sales between census years, rendering them inappropriate for our purposes. Fishback, Horrace, and Kantor (2005)
\text{study the longer run effects of New Deal spending on retail sales using Census data.}\)

\(\text{We deflate both regional output and military procurement spending using the national CPI for the United States.}\)

\(\text{A potential concern with normalizing on both sides of the regression by state-level output and population is that}
\text{measurement error in these variables might bias our results. However, we use instrumental variables that are based on}
\text{variation in national government spending and thus uncorrelated with this measurement error. This should eliminate}
\text{any bias due to measurement error. We have also run a specification where we regress the level of output growth on}
\text{the level of government spending. This yields slightly larger multipliers.}\)

\(\text{An alternative approach would be to use one-year changes in output and government spending and include lags}
\text{and leads of government spending on the right hand side. We have explored this and found that our biannual regression}
\text{captures the bulk of the dynamics in a parsimonious way. The sum of the coefficients in the dynamic specification is}
\text{somewhat larger. This is mostly due to positive coefficients on the first three leads, suggesting that there may be some}
\text{anticipatory affects. However, the standard errors on each coefficient in this specification are large and dynamic panel}
\text{regressions with fixed effects should be analyzed with care since they are in general inconsistent. Also, there may be}
\text{measurement error in the timing of the procurement spending variable we use and some of the work may actually be}
\text{carried out in the year after (or before) the year the procurement spending is recorded.}\)
1966-2006 and account for the overlapping nature of the observations in our regression by clustering the standard errors by state or region. The regional data are constructed by aggregating state-level data within Census divisions. We make one adjustment to the Census divisions. This is to divide the “South Atlantic” division into two parts because of its large size.\textsuperscript{20} This yields ten regions made up of contiguous states. Our interest focuses on the coefficient $\beta$ in regression (1), which we refer to as the “open economy relative multiplier.”

An important challenge to identifying the effect of government spending is that government spending is potentially endogenous since military spending is notoriously political.\textsuperscript{21} We therefore estimate equation (1) using an instrumental variables approach. Our instruments are based on two characteristics of the evolution of military spending. Figure 1 plots the evolution of military procurement spending relative to state output for California and Illinois as well as military procurement spending relative to total output for the U.S. as a whole.\textsuperscript{22} First, notice that most of the variation in national military spending is driven by geopolitical events—such as the Vietnam War, Soviet invasion of Afghanistan and 9/11. Second, it is clear from the figure that military spending in California is systematically more sensitive to movements in national military spending than military spending in Illinois. The 1966-1971 Vietnam War draw-down illustrates this. Over this period, military procurement in California fell by 2.5 percentage points (almost twice the national average), while military procurement in Illinois fell by only about 1 percentage point (about 2/3 the national average). We use this variation in the sensitivity of military spending across regions to national military build-ups and draw-downs to identify the effects of government spending shocks. Our identifying assumption is that the U.S. does not embark on a military build-up because states that receive a disproportionate amount of military spending are doing poorly relative to other states. This assumption is similar—but weaker than—the common identifying assumption in the empirical literature on the effects of national military spending, that variation in national military spending is exogenous to the U.S. business cycle.

We employ two separate approaches to constructing instruments that capture the differential sensitivity of military spending across regions to national military build-ups and draw-downs.\textsuperscript{23} Our baseline approach is to instrument for state or region military procurement using total national

\textsuperscript{20}We place Delaware, Maryland, Washington DC, Virginia and West Virginia in one region, and North Carolina, South Carolina, Georgia and Florida in the other.

\textsuperscript{21}See Mintz (1992) for a discussion of political issues related to the allocation of military procurement spending.

\textsuperscript{22}Below, we will sometimes refer to spending relative to GDP simply as spending and the change in spending divided by GDP simply as the change in spending, for simplicity.

\textsuperscript{23}Murtazashvili and Wooldridge (2008) derive conditions for consistency of the fixed effects instrumental variables estimator we employ for a setting in which the multiplier varies across states.
procurement interacted with a state or region dummy. The “first stage” in the two-stage least squares interpretation of this procedure is to regress changes in state spending on changes in aggregate spending and fixed effects allowing for different sensitivities across different states. This yields scaled versions of changes national spending as fitted values for each state. Table 1 lists the states for which state procurement spending is most sensitive to variation in national procurement spending. We also employ a simpler “Bartik” approach to constructing instruments (Bartik, 1991). In this case, we scale national spending for each state by the average level of spending in that state relative to state output in the first five years of our sample.\textsuperscript{24}

We estimate the effects of military spending on employment and inflation using an analogous approach. For employment, the regression is analogous to equation (1) except that the left-hand side variable is \((L_{it} - L_{it-2})/L_{it-2}\)—where \(L_{it}\) is the employment rate (employment divided by population). For the inflation regression, the left-hand side variable is \((P_{it} - P_{it-2})/P_{it-2}\), where \(P_{it}\) is the price level.

U.S. states and regions are much more open economies than the U.S. as a whole. Using data from the U.S. Commodity Flow Survey and National Income and Product Accounts, we estimate that roughly 30 percent of the consumption basket of the typical region we use in our analysis is imported from other regions (see section 4.4 for details). Even though a large majority of goods are imported, the overall level of openness of U.S. regions is modest because services account for a large fraction of output and are much more local. This estimate suggests that our regions are comparable in openness to mid-sized European countries such as Spain.

3.2 Subcontracting of Prime Military Contracts

An important question with regard to the use of prime military contract data is to what extent the interpretation of these data might be affected by subcontracting to firms in other states. Fortunately, a second source of data exists on actual shipments to the government from defense oriented industries. These data were gathered by the Census Bureau over the period 1963-1983 as an appendage to the Annual Survey of Manufacturers. They have rarely been used, perhaps because no electronic version previously existed. We digitized these data from microfilm.

Figure 2 illustrates the close relationship between these shipment data and the military procurement data for several states over this period—giving us confidence in the prime military contract

\textsuperscript{24}Nekarda and Ramey (2011) use a similar approach to instrument for government purchases from particular industries. They use data at 5 year intervals to estimate the share of aggregate government spending from different industries.
data as a measure of the timing and magnitude of regional military production. To summarize this relationship, we estimate the following regression of shipments from a particular state on military procurement,

$$MS_{it} = \alpha_i + \beta MPS_{it} + \epsilon_{it},$$

(2)

where $MS_{it}$ is the value of shipments from the Census Bureau data and $MPS_{it}$ is military procurement spending. This regression yields a point estimate of $\beta = 0.96$, indicating that military procurement moves on average one-for-one with the value of shipments. The small differences between the two series probably indicate that they both measure regional production with some error. As we discuss below, one advantage of the instrumental variables approach we adopt is that it helps adjust for this type of measurement error.

### 3.3 Effects of Government Spending Shocks

The first row of Table 2 reports the open economy relative multiplier $\beta$ in regression (1) for our baseline instruments. Standard errors are in parentheses and are clustered by states or regions.\(^{25}\) In the second row of Table 2, we present an analogous set of results using a broader measure of military spending that combines military procurement spending with compensation of military employees for each state or region. We present results for output both deflated by national CPI and our measure of state CPI.\(^{26}\)

The point estimates of $\beta$ for the output regression range from 1.4 to 1.9, while the point estimates of $\beta$ for the employment regression range from 1.3 to 1.8. The estimates using regional data are, in general, slightly larger than those based on state data, though the differences are small and statistically insignificant. The standard errors for the state regressions range from 0.3-0.4, while those for the region regressions range from 0.6-0.9. As is clear from Figure 1, the variation we use to estimate the multiplier is dominated by a few military build-ups and draw-downs.

These results control for short-term movements in population associated with government spending by running the regressions on per-capita variables. The last column of Table 2 looks directly at population movements by estimating an analogous specification to equation (1) where the left-hand side variable is $(Pop_{it} - Pop_{it-2})/Pop_{it-2}$ and the right-hand side government spending variable is constructed from the level of government spending and output rather than per-capita government

\(^{25}\)Our standard errors thus allow for arbitrary correlation over time in the error term for a given state or region. They also allow for heteroskedasticity.

\(^{26}\)When deflating by our measure of state CPI in Table 2 we impute the state CPI’s for the first two years using our baseline instrumental variables regression of state CPI on procurement spending.
spending and output. We find that the population responses to government spending shocks are small and cannot be distinguished from zero for the two year time horizon we consider.\textsuperscript{27} We also present estimates of the effects of military spending on consumer prices. These are statistically insignificantly different from zero, ranging from small positive to small negative numbers.

Figure 3 gives a visual representation of our main specification for output. The figure plots averages of changes in output against predicted military spending (based on our first-stage regression), grouped by 30 quantiles of the predicted military spending variable. Both variables are demeaned by year and state fixed effects. The vast majority of points in the figure are located in the NE and SW quadrants, leading to a positive coefficient in our IV regression. To assess the robustness of our results to outliers, we have experimented with dropping states and regions with especially large or small estimated sensitivity of spending to national spending and this slightly raises the estimated open economy relative multiplier.\textsuperscript{28}

In Table 3, we report results for the simpler “Bartik” approach to constructing instruments. For output, this approach yields an open economy relative multiplier of roughly 2.5 for the states and 2.8 for the regions. For employment, this approach also yields larger open economy relative multipliers than our baseline specification—1.8 for states and 2.5 for regions. Our estimates using the Bartik-type instruments are somewhat less precise than those using our baseline instruments. This arises because in constructing this instrument, we use the level of spending in each state as a proxy for the sensitivity of state spending to national spending—but it is an imperfect proxy.

Table 3 also reports a number of alternative specifications for the effects of military procurement on output and employment designed to evaluate the robustness of our results. We report the output multiplier when per-capita output is constructed using a measure of the working age population as opposed to the total population.\textsuperscript{29} We add the price of oil interacted with state dummies as controls to our baseline regression. We add the real interest rate interacted with state dummies as controls to our baseline regression. We estimate the employment regression using the BEA’s employment series (available from 1969) instead of BLS payroll employment. Table 3 shows that these specifications all yield similar results to our baseline estimates.

\textsuperscript{27}Our estimates appear consistent with existing estimates of regional population dynamics. Blanchard and Katz (1992) show that population dynamics are important in determining the dynamics of unemployment over longer horizons.

\textsuperscript{28}MO and CT have substantially higher estimated sensitivity of spending to national spending than other states and ND has a substantially negative estimated sensitivity (alone among the states). Dropping any combination of these states from our baseline regression slightly raises our multiplier estimate. Dropping all three yields 1.88 (0.57).

\textsuperscript{29}State-level measures of population by age-group are available from the Census Bureau starting in 1970. We define the working age population as the population between the ages of 19 and 64.
We have extensively investigated the small-sample properties of our estimation approach using Monte Carlo simulations. These simulations indicate that neither the regional regressions nor the regressions using the Bartik-type instruments suffer from bias associated with weak or many instruments. However, our estimates of the state regressions using our baseline instruments are likely to be conservative in the sense of underestimating the open economy relative multiplier for states by roughly 10 percent (implying that the true state-level open economy relative multiplier is 1.65 rather than 1.43). Intuitively, this downward bias arises because instrumental variables does not fully correct for endogeneity in small samples when instruments are weak or when many instruments are used—i.e., IV is biased in the direction of OLS. Table 3 also reports results using the LIML estimator, which is not affected by the presence of many instruments. This yields an output multiplier of roughly 2.0. Our Monte Carlo simulation also allows us to assess the small sample properties of the standard errors we report. Our simulations imply that the asymptotic standard errors for the region regressions are slightly smaller than their small-sample counterparts: the standard 95 percent confidence interval based on the standard errors reported in Table 2 is in fact a 90 percent confidence interval. This adjustment arises from the well-known small-sample bias in clustered standard errors in the presence of a small number of clusters. This does not apply to the state-level regressions for which the asymptotic standard errors almost exactly replicate the small sample results from our simulations.

A potential concern with interpreting our results would arise if states receiving large amounts of military spending were more cyclically sensitive than other states. We have compared the cyclical sensitivity of states that receive large and small amounts of military spending. The standard deviation of output growth is almost identical in states with above-median military spending and in states with below-median military spending, indicating that a difference in overall cyclical sensitivity is not

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30 See Stock, Wright, and Yogo (2002) for an overview of this issue. The concern is that the first-stage of the IV procedure may pick up some of the endogenous variation in the explanatory variable in the presence of a large number of instruments. In contrast to the canonical examples discussed in Stock, Wright, and Yogo (2002), this actually biases us away from finding a statistically significant result in small samples, since the OLS estimates in our case are close to zero. Our Monte Carlo analysis is roughly consistent with the asymptotic results reported in Stock and Yogo (2005). The partial R-squared of the excluded instruments, a statistic frequently used to gauge the “strength” of instruments is 12 percent for the state regressions and 18 percent for the region regressions. However, because we use a large number of instruments in our baseline case—one for each state or region—the Cragg-Donald (1993) first stage F-statistic suggested by Stock and Yogo (2005) is roughly 5 for our baseline specification of the state-level regressions and 8 for the region-level regressions. For the simpler Bartik-type instrument specification it is 106 for the state-level regression and 53 for the region-level regression. Our Monte Carlo analysis indicates that while the large number of instruments in the state-level specification leads to a slight downward-bias in the coefficient on government spending, the standard error on this coefficient is unbiased because of the high R-squared of our instruments taken as a whole. We thank Marcelo Moreira, James Stock and Motohiro Yogo for generous advice on this issue.

31 See Stock and Yogo (2005) for a discussion of the LIML estimator’s properties in settings with many instruments. The disadvantage of LIML is that its distribution has fat tails and, thus, yields large standard errors.
Davis, Loungani, and Mahidhara (1997) finds smaller employment multipliers when using data from the Current Population Survey (CPS) than when using CES data. They argue that this may be due to shifts in employment between the self-employed sector and more formal sectors, since self-employment is only measured in the CPS. We have run regression (1) with CPS data. In this case, the sample period is 1976-2006 and we use the Bartik-type instruments to avoid the difficulties associated with the many instrument problem discussed above given this short sample period. The point estimates using CPS data are 1.4 (0.5). Using CES data for the same sample period yields 1.8 (0.4). The estimate based on CPS data is, thus, smaller, though not significantly so. This provides some suggestive evidence of shifts between self-employment and the more formal sector.

Ramey (2011) argues that news about military spending leads actual spending by several quarters and that this has important implications for the estimation of fiscal multipliers. When we add future spending as a regressor in regression (1), the coefficient on this variable is positive and the sum of the coefficients on the government spending rises somewhat. This suggests that our baseline specification somewhat underestimates the multiplier by ignoring output effects associated with anticipated future spending.

Table 3 also presents OLS estimates of our baseline specification for output. The OLS estimates are substantially lower than our instrumental variables estimates. One potential explanation for this is that states’ elected officials may find it easier to argue for spending at times when their states are having trouble economically. Another potential explanation is that our instruments correct for measurement error in the data on state-level prime military contracts that does not arise at the national level. Such measurement error causes an “attenuation bias” in the OLS coefficient toward zero. We can assess the importance of measurement error in explaining the difference between our IV and OLS estimates by using the shipments data discussed in section 3.2 above as an instrument for the prime military contract data. For the 1966-1982 sample period for which we have the shipments data, this IV procedure yields an open economy relative multiplier of 1.3 (0.5), OLS yields 0.2 (0.2), and IV with the Bartik-type instrument yields 2.0 (0.4). This suggests that measurement error explains a substantial fraction of the difference between our IV and OLS estimates.

Furthermore, suppose we regress state output growth $\Delta Y_t$ on scaled national output growth $s_i \Delta Y_t$, where the scaling factor $s_i$ is the average level of military spending in each state relative to state output, as well as state and time fixed effects. If state with high $s_i$ are more cyclically sensitive, this regression should yield a positive coefficient on $s_i \Delta Y_t$. In fact, the coefficient is slightly negative in our data. In contrast, when $s_i \Delta Y_t$ is replaced with $s_i \Delta G_t$, this regression yields a large positive coefficient.

Since the shipments data are an independent (noisy) measure of the magnitude of spending, they will correct for measurement error. But they will not correct for endogeneity due to countercyclicality of spending.
Table 4 presents the results for equation (1) estimated separately by major SIC/NAICS groupings. An important point evident from Table 4 is that increases in government sector output contribute negligibly to the overall effects we estimate. The table also shows that increases in relative procurement spending are not associated with increases in other forms of military output. Effects on measured output in the government sector are less easily interpretable than effects on output in the private sector since much of government output is measured using input costs. Transfers associated with increases in public sector wages are therefore difficult to distinguish from changes in actual output. Statistically significant output responses occur in the construction, manufacturing, retail and services sectors.

3.4 Government Spending at High Versus Low Unemployment Rates

We next investigate whether the effects of government spending on the economy are larger in periods when the unemployment rate is already high. There are a variety of reasons why this could be the case. Most often cited is the idea that in an economy with greater slack, expansionary government spending is less likely to crowd out private consumption or investment.\(^{34}\) A second potential source of such differences is the differential response of monetary policy—central bankers may have less incentive to “lean against the wind” to counteract the effects of government spending increases if unemployment is high. We show in section 5, however, that this second effect does not affect the size of the open economy relative multiplier since aggregate policy is “differenced out.”

To investigate these issues, we estimate the following regression,

\[
\frac{Y_{it} - Y_{it-2}}{Y_{it-2}} = \alpha_i + \gamma_t + \beta_h \frac{G_{it} - G_{it-2}}{Y_{it-2}} + (\beta_l - \beta_h) I_{it} \frac{G_{it} - G_{it-2}}{Y_{it-2}} + \epsilon_{it},
\]  

(3)

where \(I_{it}\) is an indicator for a period of low economic slack, and the effects of government spending in high and low slack periods are given by \(\beta_h\) and \(\beta_l\) respectively. We define high and low slack periods in terms of the unemployment rate at the start of the interval over which the government spending occurs. We present two sets of results; one with slack defined using the national unemployment rate and the other with slack defined using the state unemployment rate.\(^{35}\)

Table 5 presents our estimates of equation (3). For output, the point estimates support the view

\(^{34}\)This might arise, for example, if unemployment leads to a higher labor supply elasticity (Hall, 2009) or because of tighter capacity constraints in booms (Gordon and Krenn, 2010).

\(^{35}\)When we base our low slack indicator \(I_{it}\) on the national unemployment rate, we set \(I_{it} = 1\) for all states in years when the national unemployment rate is below its median value over our sample. When we base \(I_{it}\) on the state unemployment rate, we set \(I_{it} = 1\) for state \(i\) in years when its unemployment rate is below its median over our sample period. When we define slack using the state unemployment rate, we interact the year and state fixed effects with the dummy.
that the effects of government spending are larger when unemployment is high. Depending on the specification, the open economy relative multiplier lies between 3.5 and 4.5 in the high slackness periods, substantially above our estimates for the time period as a whole. Given the limited number of business cycles in our sample, we are not, however, able to estimate these effects with much statistical precision. The difference in the multiplier in the high and low spending periods is only moderately statistically significant (with a P-values of 0.06 and 0.07). For employment the multiplier estimates for the high slack periods are close to those for the period as a whole and the difference in the multiplier between the high and low spending periods is relatively small and statistically insignificant.\(^{36}\)

## 4 A Model of Government Spending in a Monetary Union

In this section, we develop a framework to help us interpret the “open economy relative multiplier” that we estimate in section 3, and relate it to the “closed economy aggregate multiplier,” which has been the focus of most earlier work on government spending multipliers. Many of the issues that arise in interpreting the open economy relative multiplier also arise in the international economics literature. The model we develop, therefore, draws heavily on earlier work on open economy business cycle models (Obstfeld and Rogoff, 1995; Chari, Kehoe and McGrattan, 2002), and, in particular, the literature on monetary unions (Benigno and Benigno, 2003; Gali and Monacelli, 2008). Our model and some of our results are closely related to the analysis of Corsetti, Kuester, and Muller (2011), who discuss government spending in a small open economy with a fixed exchange rate.

The model consists of two regions that belong to a monetary and fiscal union. We refer to the regions as “home” and “foreign.” Think of the home region as the region in which the government spending shock occurs – a U.S. state or small group of states – and the foreign region as the rest of the economy. The population of the entire economy is normalized to one. The population of the home region is denoted by \(n\). Household preferences, market structure and firm behavior take the same form in both regions. Below, we describe the economy of the home region.

### 4.1 Households

The home region has a continuum of household types indexed by \(x\). A household’s type indicates the type of labor supplied by that household. Home households of type \(x\) seek to maximize their

\(^{36}\) Other recent papers that find evidence for larger multipliers during recessions include Auerbach and Gorodnichenko (2012) and Shoag (2010).
utility given by

$$E_0 \sum_{t=0}^{\infty} \beta^t u(C_t, L_t(x)), \quad (4)$$

where $\beta$ denotes the household’s subjective discount factor, $C_t$ denotes household consumption of a composite consumption good, $L_t(x)$ denotes household supply of differentiated labor input $x$. There are an equal (large) number of households of each type.

The composite consumption good in expression (4) is an index given by

$$C_t = \left[ \frac{1}{\phi_H} C_H^{\frac{\eta-1}{\eta}} + \frac{1}{\phi_F} C_F^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}, \quad (5)$$

where $C_H$ and $C_F$ denote the consumption of composites of home and foreign produced goods, respectively. The parameter $\eta > 0$ denotes the elasticity of substitution between home and foreign goods and $\phi_H$ and $\phi_F$ are preference parameters that determine the household’s relative preference for home and foreign goods. It is analytically convenient to normalize $\phi_H + \phi_F = 1$. If $\phi_H > n$, household preferences are biased toward home produced goods.

The subindices, $C_H$ and $C_F$, are given by

$$C_H = \left[ \int_0^1 c_{ht}(z) \frac{\theta}{\theta} \, dz \right]^\theta \quad \text{and} \quad C_F = \left[ \int_0^1 c_{ft}(z) \frac{\theta}{\theta} \, dz \right]^\theta \quad (6)$$

where $c_{ht}(z)$ and $c_{ft}(z)$ denote consumption of variety $z$ of home and foreign produced goods, respectively. There is a continuum of measure one of varieties in each region. The parameter $\theta > 1$ denotes the elasticity of substitution between different varieties.

Goods markets are completely integrated across regions. Home and foreign households thus face the same prices for each of the differentiated goods produced in the economy. We denote these prices by $p_{ht}(z)$ for home produced goods and $p_{ft}(z)$ for foreign produced goods. All prices are denominated in a common currency called “dollars.”

Households have access to complete financial markets. There are no impediments to trade in financial securities across regions.\footnote{Section 5.4 discusses a version of our model without incomplete financial markets across regions.} Home households of type $x$ face a flow budget constraint given by

$$P_t C_t + E_t[M_{t+1} B_{t+1}(x)] \leq B_t(x) + (1 - \tau_t) W_t(x) L_t(x) + \int_0^1 \Xi_{ht}(z) \, dz - T_t, \quad (7)$$

where $P_t$ is a price index that gives the minimum price of a unit of the consumption good $C_t$, $B_{t+1}(x)$ is a random variable that denotes the state contingent payoff of the portfolio of financial securities held by households of type $x$ at the beginning of period $t + 1$, $M_{t+1}$ is the stochastic discount factor that prices these payoffs in period $t$, $\tau_t$ denotes a labor income tax levied by the government in period
$t$, $W_t(x)$ denotes the wage rate received by home households of type $x$ in period $t$, $\Xi_{ht}(z)$ is the profit of home firm $z$ in period $t$ and $T_t$ denotes lump sum taxes.\footnote{The stochastic discount factor $M_{t,t+1}$ is a random variable over states in period $t + 1$. For each such state it equals the price of the Arrow-Debreu asset that pays off in that state divided by the conditional probability of that state. See Cochrane (2005) for a detailed discussion.} To rule out Ponzi schemes, household debt cannot exceed the present value of future income in any state of the world.

Households face a decision in each period about how much to spend on consumption, how many hours of labor to supply, how much to consume of each differentiated good produced in the economy and what portfolio of assets to purchase. Optimal choice regarding the trade-off between current consumption and consumption in different states in the future yields the following consumption Euler equation:

$$\frac{u_c(C_{t+j}, L_{t+j}(x))}{u_c(C_t, L_t(x))} = \frac{M_{t,t+j} P_{t+j}}{\beta^j} \frac{P_t}{P_{t+j}}$$

as well as a standard transversality condition. Subscripts on the function $u$ denote partial derivatives. Equation (8) holds state-by-state for all $j > 0$. Optimal choice regarding the intratemporal trade-off between current consumption and current labor supply yields a labor supply equation:

$$\frac{u_l(C_t, L_t(x))}{u_c(C_t, L_t(x))} = (1 - \tau_t) \frac{W_t(x)}{P_t}.$$ 

Households optimally choose to minimize the cost of attaining the level of consumption $C_t$. This implies the following demand curves for home and foreign goods and for each of the differentiated products produced in the economy:

$$C_{H,t} = \phi_H C_t \left( \frac{P_{Ht}}{P_t} \right)^{-\eta} \quad \text{and} \quad C_{F,t} = \phi_F C_t \left( \frac{P_{Ft}}{P_t} \right)^{-\eta},$$

$$c_{ht}(z) = C_{Ht} \left( \frac{p_t(z)}{P_{Ht}} \right)^{-\theta} \quad \text{and} \quad c_{ft}(z) = C_{Ft} \left( \frac{p_t(z)}{P_{Ft}} \right)^{-\theta},$$

where

$$P_{Ht} = \left[ \int_0^1 p_t(z)^{1-\eta} dz \right]^{\frac{1}{1-\eta}} \quad \text{and} \quad P_{Ft} = \left[ \int_0^1 p^*_t(z)^{1-\eta} dz \right]^{\frac{1}{1-\eta}},$$

and

$$P_t = \left[ \phi_H P_{Ht}^{1-\eta} + \phi_F P_{Ft}^{1-\eta} \right]^{\frac{1}{1-\eta}}.$$
where \( Q_t = P_t^*/P_t \) is the real exchange rate. This is the “Backus-Smith” condition that describes optimal risk-sharing between home and foreign households (Backus and Smith, 1993). For simplicity, we assume that all households—in both regions—initially have an equal amount of financial wealth.

4.2 The Government

The economy has a federal government that conducts fiscal and monetary policy. Total government spending in the home and foreign region follow exogenous AR(1) processes. Let \( G_{Ht} \) denote government spending per capita in the home region. Total government spending in the home region is then \( nG_{Ht} \). For simplicity, we assume that government demand for the differentiated products produced in each region takes the same CES form as private demand. In other words, we assume that

\[
g_{ht}(z) = G_{Ht} \left( \frac{p_{ht}(z)}{P_{Ht}} \right)^{-\theta} \quad \text{and} \quad g_{ft}(z) = G_{Ft} \left( \frac{p_{ft}(z)}{P_{Ft}} \right)^{-\theta}.
\]

The government levies both labor income and lump-sum taxes to pay for its purchases of goods. Our assumption of perfect financial markets implies that any risk associated with variation in lump-sum taxes and transfers across the two regions is undone through risk-sharing. (See section 5.4 for an alternative case.) Ricardian equivalence holds in our model. We describe the policy for labor income taxes in section 5.

The federal government operates a common monetary policy for the two regions. This policy consists of the following augmented Taylor-rule for the economy-wide nominal interest rate:

\[
\hat{r}^n_t = \rho_r \hat{r}^n_{t-1} + (1 - \rho_i)(\phi_\pi \hat{\pi}^{aq}_t + \phi_y \hat{y}^{aq}_t + \phi_g \hat{g}^{aq}_t),
\]

where hatted variables denote percentage deviations from steady state. The nominal interest rate is denoted \( \hat{r}^n_t \). It responds to variation in the weighted average of consumer price inflation in the two regions \( \hat{\pi}_{t}^{aq} = n\hat{\pi}_t + (1 - n)\hat{\pi}_t^* \), where \( \hat{\pi}_t \) is consumer price inflation in the home region and \( \hat{\pi}_t^* \) is consumer price inflation in the foreign region. It also responds to variation in the weighted average of output in the two regions \( \hat{y}_{t}^{aq} = n\hat{y}_t + (1 - n)\hat{y}_t^* \). Finally, it may respond directly to the weighted average of the government spending shock in the two regions \( \hat{g}_{t}^{aq} = n\hat{g}_t + (1 - n)\hat{g}_t^* \).

4.3 Firms

There is a continuum of firms indexed by \( z \) in the home region. Firm \( z \) specializes in the production of differentiated good \( z \), the output of which we denote \( y_t(z) \). In our baseline model, labor is the only variable factor of production used by firms. Each firm is endowed with a fixed, non-depreciating
The production function of firm $z$ is

$$y_t(z) = f(L_t(z)).$$  \hfill (17)

The function $f$ is increasing and concave. It is concave because there are diminishing marginal returns to labor given the fixed amount of other inputs employed at the firm. Labor is immobile across regions. Our model yields very similar results to a model in which labor and capital are assumed to be equally mobile and the government spending shock is to per capita spending. We follow Woodford (2003) in assuming that each firm belongs to an industry $x$ and that there are many firms in each industry. The goods in industry $x$ are produced using labor of type $x$ and all firms in industry $x$ change prices at the same time.

Firm $z$ acts to maximize its value,

$$E_t \sum_{j=0}^{\infty} M_{t,t+j} [p_{t+j}(z)y_{t+j}(z) - W_{t+j}(x)L_{t+j}(z)].$$  \hfill (18)

Firm $z$ must satisfy demand for its product. The demand for firm $z$’s product comes from three sources: home consumers, foreign consumers and the government. It is given by

$$y_t(z) = (nC_{Ht} + (1-n)C^*_H + nG_{Ht}) \left( \frac{p_{Ht}(z)}{P_{Ht}} \right)^{-\theta}. \hfill (19)$$

Firm $z$ is therefore subject to the following constraint:

$$(nC_{Ht} + (1-n)C^*_H + nG_{Ht}) \left( \frac{p_{Ht}(z)}{P_{Ht}} \right)^{-\theta} \leq f(L_t(z)). \hfill (20)$$

Firm $z$ takes its industry wage $W_t(x)$ as given. Optimal choice of labor demand by the firm is given by

$$W_t(x) = f\ell(L_t(z))S_t(z), \hfill (21)$$

where $S_t(z)$ denotes the firm’s nominal marginal cost (the Lagrange multiplier on equation (20) in the firm’s constrained optimization problem).

Firm $z$ can reoptimize its price with probability $1 - \alpha$ as in Calvo (1983). With probability $\alpha$ it must keep its price unchanged. Optimal price setting by firm $z$ in periods when it can change its price is

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39Section 5.5 discusses two extensions of our baseline model with investment.

40If labor and capital are equally mobile, factor movements simply affect the relative size of the regions. For example, a positive shock to the home region causes inward migration of both labor and capital and this makes the home region larger. But in per capita terms the model is identical to a model without factor mobility (save a slight change in home bias) as long as the government spending shock is defined in per-capita terms and the open economy relative multiplier is thus virtually identical. In contrast, if labor is more mobile then capital, inward migration in response to a positive government spending shock will lower the capital-labor ratio in the home region and through this channel lower the per-capita government spending multiplier (and vice versa if capital is more mobile than labor).
price implies
\[ p_t(z) = \frac{\theta}{\theta - 1} E_t \sum_{j=0}^{\infty} \frac{\alpha^j M_{t,t+j} y_{t+j}(z)}{E_t \sum_{k=0}^{\infty} \alpha^k M_{t,t+k} y_{t+k}(z)} S_{t+j}(z). \] (22)

Intuitively, the firm sets its price equal to a constant markup over a weighted average of current and expected future marginal cost.

4.4 Calibration of Preferences and Technology

We consider the following two forms for the utility function:

\[ u(C_t, L_t(x)) = C_t^{1-\sigma^{-1}} - \frac{\chi L_t(x)^{1+\nu^{-1}}}{1+\nu^{-1}}, \] (23)

\[ u(C_t, L_t(x)) = \frac{(C_t - \chi L_t(x)^{1+\nu^{-1}}/(1+\nu^{-1}))^{1-\sigma^{-1}}}{1-\sigma^{-1}}. \] (24)

In the first utility specification, consumption and labor enter separably. They are therefore neither complements nor substitutes. The second utility function is adopted from Greenwood, Hercowitz, and Huffman (1988). We refer to this utility function as representing GHH preferences. Consumption and labor are complements for households with GHH preferences. Recently, Monacelli and Perotti (2008), Bilbiie (2011), and Hall (2009) have emphasized the implications of consumption-labor complementarities for the government spending multiplier.

For both specifications of utility, we must specify values for \( \sigma \) and \( \nu \) (\( \chi \) is irrelevant when utility is separable and determined by other parameters in the GHH case). In both cases, \( \nu \) is the Frisch-elasticity of labor supply. We set \( \nu = 1 \). This value is somewhat higher than values estimated in microeconomic studies of employed workers, but relatively standard in macroeconomics. The higher value is meant to capture variation in labor on the extensive margin—such as variation in unemployment and retirement (Hall, 2009; Chetty, et al., 2011). As Hall (2009) emphasizes, assuming a high labor supply elasticity raises the government spending multiplier. For the separable utility specification, \( \sigma \) denotes the intertemporal elasticity of substitution (IES). There is little agreement within the macroeconomics literature on the appropriate values for the IES. Hall (1988) estimates the IES to be close to zero, while Bansal and Yaron (2004), Gruber (2006) and Nakamura, et al. (2013) argue for values above 1. We set \( \sigma = 1 \), which yields balanced growth for the model with separable preferences, \( \sigma = 1 \). We set the subjective discount factor equal to \( \beta = 0.99 \), the elasticity of substitution across varieties equal to \( \theta = 7 \) and the elasticity of substitution between home and foreign goods to \( \eta = 2 \).\footnote{This is the same value for \( \eta \) as is used by Obstfeld and Rogoff (2005), and only slightly higher than the values used by Backus, Kehoe, and Kydland (1994) and Chari, Kehoe, and McGrattan (2002).} Larger values of \( \eta \) yield more expenditure switching between regions in
response to regional shocks and thus lower open economy relative multipliers.

We assume the production function \( f(L_t(z)) = L_t(z)^a \) and set \( a = 2/3 \). Regarding the frequency with which firms can change their prices, we consider two cases: \( \alpha = 0 \) (i.e., fully flexible prices) and \( \alpha = 0.75 \) (which implies that firms reoptimize there prices on average once a year). Rigid prices imply that relative prices across regions respond sluggishly to regional shocks. We set the size of the home region to \( n = 0.1 \). This roughly corresponds to the size of the average region in our regional regressions (where we divide the U.S. into 10 regions). The value of the open economy relative multiplier in our model is relatively insensitive to the size of \( n \). We set the steady state value of government purchases as a fraction of output to 0.2. We log-linearize the equilibrium conditions of the model and use the methods of Sims (2001) to find the unique bounded equilibrium. By doing this we rule out the types of non-linearities we find suggestive evidence for in section 3.4.

We use data from the U.S. Commodity Flow Survey (CFS) and the U.S. National Income and Product Accounts (NIPA) to set the home-bias parameter \( \phi_H \). The CFS reports data on shipments of goods within and between states in the U.S. It covers shipments between establishments in the mining, manufacturing, wholesale and retail sectors. For the average state in 2002, 38 percent of shipments were within state and 50 percent of shipments were within region. However, roughly 40 percent of all shipments in the CFS are from wholesalers to retailers and the results of Hillberry and Hummels (2003) suggest that a large majority of these are likely to be within region. Since the relevant shipments for our model are those from manufacturers to wholesalers, we assume that 83 percent of these are from another region (50 of the remaining 60 percent of shipments).

To calculate the degree of home bias, we must account for the fact that a substantial fraction of output is services, which are not measured in the CFS. NIPA data indicate that goods represent roughly 30 percent of U.S. GDP. If all inter-region trade were in goods—i.e., all services were local—imports from other regions would amount to 25 percent of total consumption \((30\times0.83 = 25)\). However, for the U.S. as a whole, services represent roughly 20 percent of international trade. Assuming that services represent the same fraction of cross-border trade for regions, total inter-region trade is 31 percent of region GDP \((25/0.8 = 31)\). We therefore set \( \phi_H = 0.69 \). This makes our regions slightly more open than Spain and slightly less open than Portugal. We set \( \phi_H^* \) so that overall demand for home products as a fraction of overall demand for all products is equal to the size of the home population relative to the total population of the economy. This implies that \( \phi_H^* = (n/(1-n))\phi_F \).

We have so far calibrated the “fundamentals”—i.e., preferences and technology—for our model.
economy. We leave the detailed description of government policy to the next section. We wish to draw a clear distinction between fundamentals and government policy. The former determine constraints on the potential effects of government policy. In contrast, monetary and fiscal policy are under the government’s control and therefore “choice variables” from the perspective of an optimizing government, making it relevant to consider not only the policies that have persisted in the past but also the potential effects of alternative government policies.

5 Theoretical Results

In this section, we analyze the effects of government spending shocks in the model presented in section 4. We consider several different specifications for the economy’s “fundamentals” (separable vs. GHH preferences, flexible vs. sticky prices) as well as different specifications for aggregate monetary and tax policy. In the Neoclassical (flexible price) versions of the model, money is neutral implying that the specification of monetary policy is irrelevant. Tax policy is, however, important and we consider two specifications for tax policy described below. In the New Keynesian (sticky price) versions of the model, monetary policy is important and we consider three specifications of monetary policy within the class of interest rate rules described by equation (16).

The monetary policies we consider are: 1) a “Volcker-Greenspan” policy, 2) a “fixed real-rate” policy and 3) a “fixed nominal-rate” policy. These policies are designed to imply successively less “leaning against the wind” by the central bank in response to inflationary government spending shocks. The “Volcker-Greenspan” policy is meant to mimic the policy of the U.S. Federal Reserve during the Volcker-Greenspan period. For this case, we set the parameters in equation (16) to $\rho = 0.8$, $\phi_\pi = 1.5$, $\phi_y = 0.5$ and $\phi_g = 0.42$. This specification of monetary policy implies that the monetary authority aggressively raises the real interest rate to curtail the inflationary effects of a government spending shock.

Under the “fixed real-rate” policy, the central bank maintains a fixed real interest rate in response to government spending shocks. However, to guarantee price-level determinacy, the central bank responds aggressively to the inflationary effects of all other shocks. Under the “fixed nominal-rate policy,” the central bank maintains a fixed nominal interest rate in response to government spending shocks. But as with the fixed real-rate policy, it responds aggressively to the inflationary effects of all other shocks. We describe the details of how the fixed real-rate and fixed nominal-rate policies

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42 Many recent papers have estimated monetary rules similar to the one we adopt for the Volcker-Greenspan period (see, e.g., Taylor, 1993 and 1999; Clarida, Gali and Gertler, 2000).
are implemented in appendix A. The fixed nominal-rate policy is a close cousin of the zero lower bound scenario analyzed in detail in Eggertsson (2010), Christiano, Eichenbaum, and Rebelo (2011), and Mertens and Ravn (2010). It is, in a sense, the opposite of the aggressive “leaning against the wind” embodied in the Volcker-Greenspan policy because an inflationary shock generates a fall in real interest rates (since nominal rates are held constant). The fixed real-rate policy charts a middle ground.

We consider two specifications for tax policy. Our baseline tax policy is one in which government spending shocks are financed completely by lump sum taxes. Under this policy, all distortionary taxes remain fixed in response to the government spending shock. The second tax policy we consider is a “balanced budget” tax policy. Under this policy, labor income taxes vary in response to government spending shocks such that the government’s budget remains balanced throughout:

\[ nP_H G_H + (1 - n)P_F G_F = \tau \int W_t(x) L_t(x) dx, \]  

This policy implies that an increase in government spending is associated with an increase in distortionary taxes. We assume that the government spending shocks follow an AR(1) process and estimate the persistence of this process using data on aggregate military procurement spending. This yields a quarterly AR(1) coefficient of 0.933. We also in some cases consider the implications of more transitory government spending shocks.

We present results for both the closed economy aggregate multiplier that has been studied in much of the previous literature and the open economy relative multiplier that we provide estimates for in section 3 and has been the focus of much recent work using sub-regional data (Acconcia et al., 2011; Chodorow-Reich et al., 2012; Clemens and Miran, 2012; Cohen et al., 2011; Fishback and Kachanovskaya, 2010; Serrato and Wingender, 2010; Shoag, 2010; Wilson, 2011). We begin in sections 5.1 and 5.2 by describing results for the case of additively separable preferences. We then consider the case of GHH preferences in section 5.3. Finally, in section 5.5, we consider an extension of our model that incorporates investment.

5.1 The Closed Economy Aggregate Multiplier

We define the closed economy aggregate multiplier analogously to the previous literature on multipliers (e.g., Barro and Redlick, 2011) as the response of total output (combining home and foreign

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\[ \text{Our aggregate military procurement spending data is annual. We use a simulated method of moments approach to estimate the persistence of our quarterly AR(1) process. We describe this procedure in detail in appendix B.} \]
production) to total government spending, i.e., $\beta$ in the regression,

$$\frac{Y_{t}^{agg} - Y_{t-2}^{agg}}{Y_{t-2}^{agg}} = \alpha + \beta \frac{G_{t}^{agg} - G_{t-2}^{agg}}{Y_{t-2}^{agg}} + \epsilon_t,$$

(26)

where $Y_{t}^{agg}$ denotes aggregate output and $G_{t}^{agg}$ denotes aggregate government spending. This regression is identical to the one we use to measure the open economy relative multiplier—equation (1)—except that we are using aggregate variables and have dropped the time fixed effects. We calculate this object by simulating quarterly data from the model described in section 4, time-aggregating it up to an annual frequency, and running the regression (26) on this data.

The first column of table 6 reports results on the closed economy aggregate multiplier. These results clearly indicate that the closed economy aggregate multiplier is highly sensitive to aggregate monetary and tax policy – a point emphasized by Woodford (2011), Eggertsson (2010), Christiano, Eichenbaum, and Rebelo (2011), and Baxter and King (1993). In the New Keynesian model with a Volcker-Greenspan monetary policy, it is quite low—only 0.20. The low multiplier arises because the monetary authority reacts to the inflationary effects of the increase in government spending by raising real interest rates. This counteracts the expansionary effects of the spending shock. For monetary policies that respond less aggressively to inflationary shocks, the closed economy multiplier can be substantially larger. For the constant real-rate policy, the multiplier is one (Woodford, 2011). Intuitively, since the real interest rate remains constant rather than rising when spending increases there is no “crowding out” of consumption, implying that output rises one-for-one with government spending. For the constant nominal-rate policy, the multiplier is larger than one and can become very large depending on parameters. It is 1.70 if the government spending shock is relatively transient (half-life of one-year, $\rho_g = 0.85$). With more persistent government spending shocks ($\rho_g = 0.933$) becomes infinite. However, it should be kept in mind that the case we are considering is effectively assuming that the economy stays at the zero lower bound indefinitely. If the economy is expected to revert to, e.g., a Volcker-Greenspan monetary policy before some fixed future point the multiplier is finite.44 The intuition for the large multipliers with a constant nominal rate policy is that the government spending shock raises inflationary expectations, which lowers the real interest rate and thereby “crowds in” private demand.

The second panel of Table 6 presents results for the Neoclassical model. These results clearly indicate that the closed economy aggregate multiplier also depends on the extent to which the government spending is financed by contemporaneous distortionary taxes. If the spending is financed

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44 Similar issues regarding the finiteness of the zero lower bound multiplier arise in Eggertsson (2010) and Christiano, Eichenbaum, and Rebelo (2011).
by an increase in distortionary taxes in such a way as to maintain a balanced budget period-by-period (as opposed to by lump sum taxes), the multiplier falls by about a fourth to 0.32. If distortionary taxes are reduced in concert with an increase in government spending the aggregate multiplier can be substantially higher (though we do not report this in the table).

It is useful to pause for a moment to consider why price rigidity—the feature that distinguishes the New Keynesian and Neoclassical models we consider—matters so much in determining effects of government spending. For concreteness, consider a transitory shock to government spending at the zero lower bound. This shock puts pressure on prices to rise. In the Neoclassical model with a constant money supply, prices immediately jump up and begin falling. This implies that the real interest rate rises on impact (because prices are falling) and crowds out private spending. In the New Keynesian model, however, prices rise only gradually since many are rigid in the short run. This implies that the real interest rate falls on impact and thus boosts private spending. It is this difference in the response of the real interest rate to government spending shocks—caused by a difference in the flexibility of prices—that explains the difference in the multiplier across these models.

The sensitivity of the closed economy aggregate multiplier to aggregate monetary and tax policy probably explains some of the wide range of estimates in the empirical literature. Most economists agree that the extent to which the Federal Reserve has “leaned against the wind” has varied substantially over the last century (see, e.g., Clarida et al., 2000). This sensitivity carries over to other variables. Much recent work on the effects of fiscal policy has focused on consumption, real wages and markups (Ramey, 2011; Perotti, 2007). In our New Keynesian model with Volcker-Greenspan monetary policy, the closed economy aggregate multiplier is negative for all three of these variables, while it is positive for more accommodative monetary policy.

The enormous variation in possible values for the closed economy aggregate multiplier depending on the policy environment underscores the difficulty of using the closed economy aggregate multiplier to distinguish among alternative views of how government spending affects the economy. Under “normal” monetary policy (i.e., the Volcker-Greenspan policy), it may be exceedingly difficult to distinguish between the Neoclassical and New Keynesian models. Both frameworks predict little effect of government spending on output. Yet this does not imply that the models have similar implications overall. While the Neoclassical model continues to generate a low aggregate multiplier in the fixed nominal-rate scenario that we use to proxy for the zero lower bound, the New Keynesian model can generate extremely large multipliers in this environment. In the next section, we illustrate that the open economy relative multiplier has important advantages when it comes to distinguishing
between different views of how government spending affects the economy, because it is not sensitive to the specification of aggregate monetary and tax policy but rather to the relative policies across regions—which are precisely pinned down in a monetary and fiscal union.

5.2 The Open Economy Relative Multiplier

Contrast the wide range of different closed economy aggregate multipliers produced by our model for different monetary policies with the complete stability of the open economy relative multiplier reported in the second column of Table 6. The open economy relative multiplier is calculated by estimating equation (1) using the regional data from the model—the same specification we use in our empirical analysis. For all three specifications of monetary policy we consider, the open economy relative multiplier is 0.83. Furthermore, the fifth and sixth row of Table 6 present result for the different specifications of tax policy in the Neoclassical model and illustrate that the open economy relative multiplier is also completely insensitive to aggregate tax policy. The open economy relative multiplier is sensitive to economic fundamentals (e.g., the degree of price rigidity) and to region-specific policies (e.g., the persistence of the regional government spending shock) as we discuss below.

Intuitively, the open economy relative multiplier is independent of aggregate policy because we “difference out” aggregate shocks and aggregate policy by including time fixed effects in the regression. In a monetary union, the monetary authority cannot respond to a shock in one region by making monetary policy tighter in that region alone. The relative monetary policy between the two regions is, therefore, held fixed by the monetary union in a very precise way, regardless of the stance of aggregate monetary policy. In this sense, the open economy relative multiplier is akin to the closed economy aggregate multiplier for a relatively accommodative aggregate monetary policy—more accommodative than U.S. monetary policy under Volcker and Greenspan.

The open economy relative multiplier is smaller than one for a wide range of parameters in our model. This is most easily seen by considering the “Backus-Smith” risk-sharing condition \( c_t - c_t^* = \sigma q \). An increase in home government spending will increase the relative price of home goods and therefore decrease the “real exchange rate” \( Q_t = P_t^*/P_t \). By the Backus-Smith condition, this implies that home consumption must fall relative to foreign consumption. In other words, government spending “crowds out” private spending in relative terms implying a relative multiplier that is smaller than one.

Since the relative nominal interest rate is constant in response to a regional government spending

\[\text{Footnote: Specifically, we take a linear approximation of the dependent and independent variations equation (1) and run the regression using these approximate variables. See appendix C for details.}\]
shock, it is tempting to think that this situation is analogous to the zero lower bound, where the nominal interest rate is fixed at zero in response to government spending shocks. As in the zero lower bound case, an increase in relative government spending in the home region can raise expected inflation, lowering relative short-term real interest rates. However, unlike the zero lower bound case, the relative long-term real interest rate does not fall in response to a fiscal shock. The fiscal shock leads to an immediate rise in relative prices and expectations of further increases in the short term. This lowers the relative short term real interest rate. However, since a transitory shock to spending does not lead to a permanent change in relative prices and the exchange rate is fixed within the monetary union, any short term increase in prices in one region relative to the other region must be undone by a fall in relative prices in that region later on.\textsuperscript{46} In fact, after their initial jump, relative prices are anticipated to fall more in the long run than they are anticipated to rise further in the short run. This implies that the relative long-term real interest rate actually rises slightly in the home region in response to an increase in government spending.\textsuperscript{47}

To more clearly see the intuition for this result, Figure 4 presents the impulse response of the price level and the real interest rate in the home region relative to the foreign region after a government spending shock in our model. The home price level rises for several periods, but then falls back to its original level. This movement in prices implies that the real interest rate in the home region initially falls, but then rises above its steady state level for a prolonged period. Figure 5 shows what happens to consumption in the home region relative to the foreign region after a government spending shock. Despite the short-run fall in the real interest rate, consumption falls. This is because households anticipate high real rates in the future—equivalently, they face a high current long-term real interest rate—and therefore cut their consumption.

Since the relevant interest rate for consumption decisions—the long-term real interest rate—actually rises slightly in response to an increase in government spending irrespective of the persistence of the shock and other parameters, the fixed relative nominal interest rate policy in a monetary union is fundamentally different from a zero lower bound setting in a closed economy in which the long-term real interest rate falls in response to a government spending shock. The response of relative long-term real interest rates in our setting is closest to the fixed \textit{real} interest rate case in the closed economy setting. Table 6 shows that the open economy relative multiplier is, in fact, 0.83 for

\textsuperscript{46}Parsley and Wei (1996) present evidence for rapid convergence of relative prices following regional shocks using data for U.S. regions.

\textsuperscript{47}Corsetti, Kuester, and Muller (2011) show that the same logic holds for the case of a small open economy with a fixed exchange rate.
our baseline parameter values. This is far below the zero lower bound multipliers emphasized by Eggertsson (2010) and Christiano, Eichenbaum, and Rebelo (2011), but just slightly lower than the closed economy aggregate multiplier for a fixed real rate monetary policy.

5.3 Model with GHH Preferences

The models we have considered so far have generated predictions for the open economy relative multiplier substantially below the point estimate of roughly 1.5 that we obtained in section 3. We next consider a model with GHH preferences that is capable of fitting this feature of our empirical estimates. GHH preferences imply that consumption and labor are complements. This complementarity is intended to represent the extra consumption on food away from home, clothing, gas and the like that often arises in the context of work (Aguiar and Hurst (2005) and Aguiar, Hurst, and Karabarbounis (2012) present empirical evidence for such complementarities).

Previous work by Monacelli and Perotti (2008), Bilbiie (2011) and Hall (2009) has shown that allowing for complementarities between consumption and labor can have powerful implications for the government spending multiplier. The basic intuition is that, in response to a government spending shock, households must work more to produce the additional output. This raises consumption demand since consumption is complementary to labor. But to be able to consume more, still more production must take place, further raising the effects on output.

The second column of table 7 presents estimates of the open economy relative multiplier for the model with GHH preferences. The New Keynesian model with GHH preferences can match our empirical findings in section 3 of an open economy multiplier of roughly 1.5 (assuming a quarterly persistence of $\rho_g = 0.933$ as in the military spending data). As in the model with separable preferences, this statistic is entirely insensitive to the specification of aggregate policies. For the case of more transitory government spending shocks ($\rho_g = 0.5$), the open economy relative multiplier rises to 2.0. The Neoclassical model, however, continues to generate a low multiplier (0.3) in this model.

Figure 6 plots relative output and consumption in the New Keynesian model with GHH preferences after a positive shock to home government spending. Both output and consumption rise on impact by a little more than twice the amount of the shock. They then both fall more rapidly than

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48 Models with hand-to-mouth consumers of the type studied by Gali, Lopez-Salido, and Valles (2007) may also have the potential to generate large open economy relative multipliers.

49 Schmitt-Grohe and Uribe (2012) estimate a rich business cycle model with Jaimovich and Rebelo (2009) preferences—which nests GHH and King and Rebelo (1988) preferences as special cases. The values that they estimate for the preference parameters of their model are those for which Jaimovich-Rebelo preferences reduce to GHH preferences.
the shock. The fact that the initial rise in consumption is as large as the rise in output—which is partly fulfilling increased orders from the government—implies that the home region responds to the shock by running a trade deficit in the short run. Consumption eventually falls below its steady state level for a period of time. During this time, the home region is running a trade surplus. Intuitively, the complementarity between consumption and labor implies that home households want to shift their consumption towards periods of high work effort associated with positive government spending shocks.

How does the introduction of GHH preference affect the closed economy aggregate multiplier? The first column of Table 7 reports the closed economy aggregate multiplier in our model with GHH preferences. Under certain circumstances—in particular, the case of a fixed nominal rate rule meant to proxy for the zero lower bound—this model can generate an extremely large closed economy aggregate multiplier. However, if monetary policy is highly responsive to output as in the case of Volcker-Greenspan policy, the New Keynesian model with GHH preferences implies a low closed economy aggregate multiplier, just as the Neoclassical model does.

Table 7 makes clear that the introduction of GHH preferences does not generically increase the closed economy aggregate multiplier. In the Neoclassical model, introducing GHH preferences lowers the closed economy aggregate multiplier (to zero) by eliminating the wealth effect on labor supply.\textsuperscript{50} The introduction of GHH preferences also lowers the closed economy aggregate multiplier in the New Keynesian model when monetary policy responds aggressively to the inflationary effects of government spending shocks—as in the case of the Volcker-Greenspan policy rule. For this policy, the endogenous increase in real interest rates chokes off the chain of increases in output, employment and consumption that otherwise generates a large multiplier in the GHH model. A key reason why the introduction of GHH preferences raises the open economy relative multiplier when compared to the case of separable preferences is thus that the monetary union implies an accommodative “relative” monetary policy—sufficiently accommodative not to choke off the increase in relative output.

Summing up our results thus far, our estimates of equation (1) based on the military procurement data yield an open economy relative multiplier of roughly 1.5. This lies far above the open economy relative multipliers for the Neoclassical model—which are below 0.5 for both separable preferences and GHH preferences. Our empirical estimate of 1.5 is also substantially higher than the open economy relative multiplier of 0.83 implied by the New Keynesian model with separable preferences.

\textsuperscript{50}In the New Keynesian model, government spending shocks affect the markup of prices over marginal costs and therefore affect output by shifting labor demand. Similarly, the open economy relative multiplier in the Neoclassical model with GHH preferences is non-zero because the government spending shock shifts the labor supply curve as function of the real product wage.
The New Keynesian model with GHH preferences, however, is able to match the open economy relative multiplier we estimate in the data. Our results are thus consistent with a model in which demand shocks can have large effects on output—if monetary policy is sufficiently accommodative (as it is at the zero lower bound).

5.4 Model with Incomplete Financial Markets

The model we develop in section 4 features complete financial markets across regions of the economy. This implies that all risk associated with differential taxes and labor income across regions—possibly arising from government spending shocks—is perfectly shared. In a recent paper, Farhi and Werning (2012) have shown that in a monetary union with incomplete financial markets across regions, regional government spending multipliers can differ substantially depending on whether the spending is financed by local taxes or federal taxes. Table 8 presents open economy relative multipliers for a version of our model in which the only financial asset that is traded across regions is a non-contingent bond. For this model, we present results for two assumptions about how spending is financed: locally financed spending and federally financed spending.

Table 8 shows that these two versions of the incomplete markets model yield similar results about the open economy relative multiplier to the baseline complete markets model. In the case of federally financed spending, the open economy relative multiplier rises to 0.90 when prices are sticky. The intuition for this is that home agents are wealthier as a result of the government spending (they receive labor income far in excess of the extra taxes they must pay). Since their preferences are home-biased, their increased wealth increases home demand. In the long run, the increased wealth reduces labor supply. But the first of these effects outweighs the latter implying that the multiplier increases.

What is perhaps more surprising is that even in the case of locally financed spending the incomplete markets model yields a slightly larger open economy relative multiplier than the complete markets model when prices are sticky. In this case, home agents are not wealthier due to the government spending shock. However, they are wealthier than they would have been had they shared all risk. The reason is that the government spending shock leads to an increase in the relative price of home goods. Since home households have a stronger preference for home goods than foreign households, it is efficient for them to purchase state contingent assets that pay out when home goods are cheap and require them to pay when home goods are expensive. A home government spending shock therefore leads to a negative transfer for home agents under complete markets.
When prices are flexible, the open economy relative multiplier is slightly lower in the incomplete markets model than it is with complete markets. With flexible prices, the increase in wealth associated with the government spending reduces labor supply, whereas it does not lead to a Keynesian increase in aggregate demand. This reduction in labor supply decreases the open economy relative multiplier.

The effects of changes in wealth on the open economy relative multiplier are sensitive to the elasticity of substitution between home and foreign goods. Our baseline value for this parameter is 2. If we instead assume that this elasticity is 1, the open economy relative multiplier rises to 1.05 for federally financed spending. To be able to generate an open economy relative multiplier of 1.5, we must assume that this elasticity is below 0.6. This is a substantially lower value than most empirical studies suggest.

5.5 Models with Variable Capital

The model we develop in section 4 abstracts from investment and capital accumulation. In appendixes D and E we incorporate investment and capital accumulation into our model in two different ways. The specification presented in appendix D follows closely the setup in Woodford (2003, 2005). In this model capital is firm-specific in that each firm owns its capital stock and faces convex investment adjustment costs at the firm level. Our baseline model is a limiting case of this model when the capital share goes to zero. This setup has been used, e.g., by Eichenbaum and Fisher (2007) and Altig et al. (2011). The specification presented in appendix E largely mirrors Christiano, Eichenbaum, and Evans (2005). In this case, households own the capital stock and firms rent capital on a period-by-period basis in a frictionless regional capital market. This specification also allows for variable capital utilization and investment adjustment costs at the regional level.

Table 9 presents open economy relative multipliers for these models in the case when households have GHH preferences. The output multiplier for the firm-specific capital model is slightly larger than for our baseline model. Since the government spending shock is persistent, firms expect a high marginal return on capital for some time and increase investment when the shock occurs. In contrast, the model with regional capital markets yields a smaller multiplier than the baseline model. This occurs despite investment rising as in the firm-specific capital model. The main reason for the fall in the multiplier is that the regional nature of the capital market reduces the degree of strategic complementarity of the price setting decisions across firms relative to the baseline model (since firms that raise their price can costlessly reduce the amount of capital they rent). Clearly,
the assumption that firms rent the capital that they use each period on frictionless regional capital markets is unrealistic. Eichenbaum and Fisher (2007) and Altig et al. (2011) show that adopting the more realistic setting of firm-specific capital helps New Keynesian models with capital match the sluggish response of prices to aggregate disturbances without resorting to unrealistic assumptions about the frequency of price adjustment or the indexing of prices. The final row of Table 9 shows that with flexible prices, the open economy relative multiplier is close to zero in the firm-specific capital model. Table 9 also presents open economy relative multipliers for CPI inflation. The New Keynesian models generate small increases in relative inflation. This lines up well with our empirical findings on relative inflation. In contrast, the model with flexible prices counter-factually implies a much sharper rise in relative inflation rates.

5.6 Welfare

The welfare consequences of government spending depend not only on the multiplier, but also on the utility agents derive from the goods and services purchased by the government. Woodford (2011) and Werning (2012) provide an extensive discussion of the welfare consequences of government spending. To illustrate the main forces, suppose household utility can be represented by \( U(C_t, L_t, G_t) \) and the production function is \( Y_t = f(L_t) \).\(^{51}\) Household utility may then be written as \( U(Y_t - G_t, f^{-1}(Y_t), G_t) \). Following Woodford (2011), we can differentiate this and get

\[
\frac{dU}{dG} = \left( U_C - \frac{-U_L}{f_L} \right) \frac{dY}{dG} + (U_G - U_C). \tag{27}
\]

The first term is the difference between the marginal utility of consumption and the marginal disutility of producing goods \( U_L \) is negative, multiplied by the government spending multiplier. In a frictionless economy, this term is zero since output is chosen optimally to equate the two terms in the bracket. The second term is the difference between the marginal value of government spending and the marginal value of private spending. In a frictionless economy, thus, the government should spend up to a point where the value of an extra dollar of government spending is equal to that of private spending.

In an economy with frictions, output might, however, be below its optimal level making the first term positive. In this case, it may be desirable, other things equal, to increase spending beyond the point at which the second term is equal to zero. The extent of extra desirable spending will depend on the size of the multiplier, with a larger multiplier implying that more spending is desirable.

\(^{51}\)For simplicity, we abstract from investment, heterogeneous labor markets, and price dispersion due to price rigidity. And we assume that government spending is financed by lump-sum taxes.
Woodford (2011) argues that monetary policy should be the tool of choice to eliminate such “output gaps” since there is no cost to using monetary policy, and this allows fiscal policy to focus on equalizing the marginal value of an extra dollar of government spending and private spending. If fiscal policy is used to eliminate output gaps, this may interfere with that second objective. Only when monetary policy is constrained—such as when the nominal interest rate is at its zero lower bound—should fiscal policy be used to eliminate output gaps. In an economy with price rigidity, welfare is also affected by the extent of inefficient price dispersion due to inflation and government spending can raise welfare to the extent it can help stabilize inflation. Werning (2012) decomposes optimal stimulus spending into an “opportunistic” part, which reflects the desire of the government to take advantage of low prices during recessions, and a true “stimulus” part, which reflects additional spending beyond this benchmark. He argues that an important part of optimal stimulus at the zero lower bound is “opportunistic” and that “stimulus” spending may optimally be zero or close to zero.

6 Conclusion

We exploit regional variation in military spending in the US to estimate the effect of government spending on output in a monetary union. We use the fact that when the U.S. embarks upon a military buildup, there is a systematic tendency for spending to increase more in some states than others. For example, when aggregate military spending in the US rises by 1 percent of GDP, military spending in California on average rises by about 3 percent of California GDP, while military spending in Illinois rises by only about 0.5 percent of Illinois GDP. Under the assumption that the US doesn’t embark upon military buildups like the Vietnam War because states like California are doing badly relative to states like Illinois, we can use regional variation associated with these buildups to estimate the effect of a relative increase in spending on relative output. We find that when relative spending in a state increases by 1 percent of GDP, relative state GDP rises by 1.5 percent.

At first glance, this multiplier estimate may seem quite large. However, it pertains to a different object than the conventional “close economy aggregate multiplier,” in that it measures the effect of a relative change in government spending in two different states on the relative change in output. We coin the term the “open economy relative multiplier” for this object and develop a theoretical framework for interpreting how it relates to the more commonly studied aggregate government multiplier. This framework is useful in interpreting the growing number of studies that attempt to use regional variation to measure the government spending multiplier (e.g., Accoucia et al., 2011; Chodorow-Reich et al., 2012; Clemens and Miran, 2012; Cohen et al., 2011; Fishback and Kachanovskaya, 2010;...
Serrato and Wingender, 2010; Shoag, 2010; Wilson, 2011).

We show that the open economy relative multiplier is a sharp diagnostic tool in distinguishing among alternative macroeconomic models. The closed economy aggregate multiplier is highly sensitive to how aggressively monetary and tax policy “lean against the wind” in response to a government spending shock, with the multiplier being larger if policy is more accommodative. In contrast, since the open economy relative multiplier focuses on relative changes in government spending and output, these aggregate factors are “differenced out,” allowing for much sharper theoretical predictions.

We show that our estimates are much more consistent with New Keynesian models in which “aggregate demand” shocks—such as government spending shocks—have potentially large effects on output than they are with the plain-vanilla Neoclassical model. In particular, our results suggest that government spending should have large output multipliers when the economy is in a liquidity trap, i.e., the nominal interest rate hits its lower bound of zero and becomes unresponsive to economic shocks. This scenario is particularly relevant in the context of the near zero nominal interest rates that have prevailed in many countries in recent years.
A Constant Real and Nominal Rate Monetary Policies

The paper considers specifications of monetary policy that hold the real or nominal interest rate constant in response to a government spending shock. Here, we illustrate the method used to solve for these monetary policy specifications. We do this for the case of separable preference. We use an analogous approach for the case of GHH preference.

Consider the closed economy limit of our model. A log-linear approximation of the key equilibrium conditions of this model are

\[ 
\hat{c}_t = E_t \hat{c}_{t+1} - \sigma (\hat{r}_t^n - E_t \hat{\pi}_{t+1}), 
\]

\[ \hat{\pi}_t = \beta E_t \hat{\pi}_{t+1} + \kappa \zeta (\hat{c}_t + \kappa \zeta \psi_y \hat{y}_t), \]

\[ \hat{y}_t = \left( \frac{C}{Y} \right) \hat{c}_t + \hat{g}_t, \]

where \( \zeta = 1/(1 + \psi \nu) \) and \( \psi_y = (1 + \nu^{-1})/a - 1. \)

Using equation (30) to eliminate \( \hat{y}_t \) from equations (28) and (29) yields

\[ 
\hat{c}_t = E_t \hat{c}_{t+1} - \sigma (\hat{r}_t^n - E_t \hat{\pi}_{t+1}), 
\]

\[ \hat{\pi}_t = \beta E_t \hat{\pi}_{t+1} + \kappa \zeta \hat{c}_t + \kappa \zeta \hat{g}_t, \]

where \( \zeta_y = \zeta (\sigma^{-1} + (C/Y)\psi_y) \) and \( \zeta_g = \zeta \psi_y. \) Recall that \( \hat{g}_t = \rho_g \hat{g}_{t-1} + \epsilon_{g,t}. \)

A.1 Fixed Real Rate Monetary Policy

An equilibrium with a fixed real interest rate must satisfy

\[ 
\hat{c}_t = E_t \hat{c}_{t+1}, 
\]

\[ \hat{\pi}_t = \beta E_t \hat{\pi}_{t+1} + \kappa \zeta \hat{c}_t + \kappa \zeta \hat{g}_t. \]

We conjecture a solution of the form \( \hat{c}_t^* = a_c \hat{g}_t, \hat{\pi}_t^* = a_\pi \hat{g}_t. \) Using the method of undetermined coefficients, it is easy to verify that such an equilibrium exists with

\[ 
a_c = 0, \quad a_\pi = \kappa \frac{\zeta_y}{1 - \rho_g}. \]

This equilibrium can be implemented with the following policy rule

\[ 
\hat{r}_t^n = E_t \hat{\pi}_{t+1} + \phi_\pi (\hat{\pi}_t - \hat{\pi}_t^*) 
= a_\pi \rho_g \hat{g}_t + \phi_\pi \hat{\pi}_t - a_\pi \phi_\pi \hat{g}_t 
= \phi_\pi \hat{\pi}_t - a_\pi (\phi_\pi - \rho_g) \hat{g}_t. \]
A.2 Fixed Nominal Rate Monetary Policy

An equilibrium with a fixed nominal interest rate must satisfy

\[ \hat{c}_t = E_t \hat{c}_{t+1} + \sigma E_t \hat{\pi}_{t+1}, \]  
\[ \hat{\pi}_t = \beta E_t \hat{\pi}_{t+1} + \kappa \zeta \hat{c}_t + \kappa \zeta \hat{g}_t. \]  
\[ (36) \]
\[ (37) \]

We again conjecture a solution of the form \( \hat{c}_t^* = a_c \hat{g}_t, \hat{\pi}_t^* = a_\pi \hat{g}_t \). Using the method of undetermined coefficients, it is easy to verify that such an equilibrium exists with

\[ a_c = \frac{\rho_g \kappa \zeta_c}{A_c}, \quad a_\pi = \kappa \frac{\zeta_c}{1 - \beta \rho_g} a_c + \kappa \frac{\zeta_c}{1 - \beta \rho_g}. \]

where \( A_c = (1 - \rho_g) (1 - \beta \rho_g) - \rho_g \kappa \zeta_c \). This solution is however only valid when \( A_c > 0 \). For \( 0 < \rho_g < 1 \), \( A_c \) is decreasing in \( \rho_g \). There is a critical point at which \( A_c = 0 \). As \( \rho_g \) rises and \( A_c \) falls towards zero, \( a_c \to \infty \). For values of \( \rho_g \) that are above this point, our solution method breaks down since \( a_c \) is infinite. Similar parameter restrictions arise in Eggertsson (2010) and Christiano, Eichenbaum, and Rebelo (2011).

In the valid range, this equilibrium can be implemented with the following policy rule

\[ \hat{r}_n = \phi \hat{\pi}_t - a_\pi \phi \hat{g}_t. \]  
\[ (38) \]

B Persistence of the Government Spending Shocks

We use annual data on aggregate military procurement spending to calibrate the persistence of the government spending shocks that we feed into our model. The first order autocorrelation of aggregate military procurement spending suggests a great deal of persistence. However, higher order autocorrelations suggest less persistence. To capture this behavior in a parsimonious way, we estimate a quarterly AR(1) process by simulated method of moments using the first five autocorrelations as moments.

More specifically, our procedure is the following. First, we take the log of aggregate military procurement spending and detrend it (results are insensitive to this). We then estimate regressions of the following form:

\[ G_t^{agg} = \alpha_j + \beta_j G_{t-j}^{agg} + \epsilon_t, \]

where \( G_t^{agg} \) is detrended log aggregate military procurement spending. We use \( \beta_j \) for \( j = 1, ..., 5 \) as the moments in our simulated methods of moments estimation. We then simulate quarterly
data from AR(1) processes with different degrees of persistence, time aggregate these data to an annual frequency, and run these same regressions on the simulated data. We then find the value of the quarterly AR(1) parameter that minimizes the sum of the squared deviations of the empirical moments from the simulated moments.

C Linear Approximation of Equation (1) for Model Regressions

To calculate the open economy relative multiplier for simulated data from our model, we must take a linear approximation of the dependent and independent variables in equation (1) so as to be able to express the variables in the regression in terms of the variables in our model. For the output regression, we approximate the specification in which we deflate regional GDP by the regional CPI (The second specification in Table 2). The linear approximation of the dependent variable is

$$\frac{P_{Ht} Y_t - P_{Ht-2} Y_{t-2}}{P_{Ht-2} Y_{t-2}} = \frac{Y_t}{Y_{t-2}} \frac{\Pi_{Ht} \Pi_{Ht-1}}{\Pi_{t-1}} - 1 = \hat{y}_t - \hat{y}_{t-2} + \hat{\pi}_{Ht} + \hat{\pi}_{Ht-1} - \hat{\pi}_t - \hat{\pi}_{t-1} + \text{h.o.t},$$

(39)

where h.o.t. denotes “higher order terms.” The linear approximation of the independent variable is

$$\frac{P_{Ht} G_{Ht} - P_{Ht-2} G_{Ht-2}}{P_{Ht-2} Y_{t-2}} = \frac{G_{Ht}}{Y_{t-2}} \frac{\Pi_{Ht} \Pi_{Ht-1}}{\Pi_{t-1}} - \frac{G_{Ht-2}}{Y_{t-2}}$$

$$= \hat{g}_t - \hat{g}_{t-2} + \left(1 - \frac{C}{Y}\right) (\hat{\pi}_{Ht} + \hat{\pi}_{Ht-1} - \hat{\pi}_t - \hat{\pi}_{t-1}) + \text{h.o.t}. \quad (40)$$

D A Model with Firm-Specific Capital

This appendix presents a model of investment and capital accumulation that mirrors closely the specification in Woodford (2003, 2005). In this model, firms own their capital stock and face adjustment costs at the firm level in adjusting their capital stock. Household behavior is governed by the same equations as in our baseline model presented in section 4. As in our baseline model, firms belong to industries $x$, which make use of a specific type of labor. The production function of firms in industry $x$ is

$$y_t(x) = f(L_t(x), K_t(x)).$$

(41)

The demand for the output of firms in industry $x$ is given by

$$y_t(x) = (nC_{Ht} + (1 - n)C^*_{Ht} + nI_{H,t} + (1 - n)I^*_{H,t} + nG_{Ht}) \left(\frac{p_{ht}(x)}{P_{Ht}}\right)^{-\theta}.$$ 

(42)
Firms’ optimal choice of labor demand implies

\[ W_t(x) = f_t(L_t(x), K_t(x)) S_t(x). \]  

(43)

Each firm faces convex adjustment costs for investment. A firm that would like to choose a capital stock \( K_{t+1}(x) \) for period \( t+1 \) must invest \( I(K_{t+1}(x)/K_t(x))K_t(x) \) at time \( t \). For simplicity, assume that \( I_t \) is a composite investment good given by an index of all the products produced in the economy analogous to equations (5)-(6) for consumption. We assume that \( I(1) = \delta, I'(1) = 1, \) and \( I''(1) = \epsilon_\psi \).

Optimal investment by firms implies

\[ I_t \left( \frac{K_{t+1}(x)}{K_t(x)} \right) + E_t \frac{P_{t+1}}{P_t} \left[ I \left( \frac{K_{t+2}(x)}{K_{t+1}(x)} \right) - I' \left( \frac{K_{t+2}(x)}{K_{t+1}(x)} \right) \frac{K_{t+2}(x)}{K_{t+1}(x)} \right] = E_t \frac{P_{t+1}}{P_t} \frac{R^k_{t+1}(x)}{P_{H,t+1}} \frac{P_{H,t+1}}{P_{t+1}}, \]  

(44)

where

\[ R^k(x) = f_k(L_t(x), K_t(x)) S_t(x). \]  

(45)

Firm price setting is given by equation (22). This model has two new parameters relative to our baseline model. We follow Woodford (2003, 2005) in setting \( \delta = 0.012 \) and \( \epsilon_\psi = 3 \). Our results are virtually identical if we instead set \( \delta = 0.025 \) and \( \epsilon_\psi = 2.5 \). We assume that the production function is Cobb-Douglas with a capital share of 1/3.

### E Model with Regional Capital Markets

This appendix presents an extension of the model presented in section 4 that incorporates investment, capital accumulation and variable capital utilization in a way that mirrors closely the specification in Christiano, Eichenbaum, and Evans (2005). An important feature of this model is that firms rent capital on a period-by-period basis in a regional capital market.

#### E.1 Households

Household preferences in the home region are given by equations (4)-(6) as before. Household decisions regarding consumption, saving and labor supply are thus the same as before. However, in addition to these choices, households own the capital stock, they choose how much to invest and they choose the rate of utilization of the capital stock. Let \( \tilde{K}_t \) denote the physical stock of capital available for use in period \( t \) and \( I_t \) the amount of investment chosen by the household in period \( t \). For simplicity, assume that \( I_t \) is a composite investment good given by an index of all the products
produced in the economy analogous to equations (5)-(6) for consumption. The capital stock evolves according to

\[ \bar{K}_{t+1} = (1 - \delta)\bar{K}_t + \Phi(I_t, I_{t-1}), \]  

(46)

where \( \delta \) denotes the physical depreciation of capital and \( \Phi \) summarizes the technology for transforming current and past investment into capital. Households choose the utilization rate \( u_t \) of the capital stock. The amount of capital services provided by the capital stock in period \( t \) is then given by \( K_t = u_t\bar{K}_t \).

The budget constraint of households in the home region is given by

\[ P_tC_t + P_tI_t + P_tA(u_t)\bar{K}_t + E_t[M_{t,t+1}B_{t+1}(x)] \leq B_t(x) + W_t(x)L_t(x) + R^k_tu_t\bar{K}_t + \int_0^1 \Xi_{ht}(z)dz - T_t. \]  

(47)

The differences relative to the model presented in section 4 are the following. First, households spend \( P_tI_t \) on investment. Second, they incur a cost \( P_tA(u_t)\bar{K}_t \) associated with utilizing the capital stock. Here \( A(u_t) \) denotes a convex cost function. Third, they receive rental income equal to \( R^k_tu_t\bar{K}_t \) for supplying \( u_t\bar{K}_t \) in capital services to firms. Here \( R^k_t \) denotes the rental rate for a unit of capital services.

In addition to equations (8)-(11), (14) and a standard transversality condition, household optimization yields the following relevant optimality conditions. Optimal capital utilization sets the marginal cost of additional utilization equal to the rental rate on capital,

\[ A'(u_t) = \frac{R^k_t}{F_t}. \]  

(48)

Optimal investment and capital accumulation imply

\[ D_t\Phi_1(I_t, I_{t-1}) + \beta E_t[D_{t+1}\Phi_2(I_{t+1}, I_t)] = u_c(C_t, L_t(x)), \]  

(49)

\[ D_t = \beta(1 - \delta)E_tD_{t+1} + \beta E_t[A'(u_{t+1})u_{t+1} - A(u_{t+1})u_c(C_{t+1}, L_{t+1}(x))], \]  

(50)

where \( D_t \) is the Lagrange multiplier on equation (46) and \( \Phi_j(\cdot, \cdot) \) denotes the derivative of \( \Phi \) with respect to its \( j \)th argument.

E.2 Firms

The production function of firms in industry \( x \) and the demand for the output of firms in industry \( x \) is given by equations (41) and (42) as in the firm-specific capital model presented in appendix D.
Firms’ optimal choice of labor demand yields equation (43). Firms’ optimal capital demand implies

\[ R^k_t = f_k(L_t(z), K_t(z))S_t(z). \] (51)

Firm price setting is given by equation (22).

E.3 Calibration

We set the rate of depreciation of capital to \( \delta = 0.025 \), which implies an annual depreciation rate of 10 percent. The investment adjustment cost function is given by

\[ \Phi(I_t, I_{t-1}) = \left[ 1 - \phi \left( \frac{I_t}{I_{t-1}} \right) \right] I_t, \] (52)

where \( \phi(1) = \phi'(1) = 0 \) and \( \kappa_I = \phi''(1) > 0 \). We set \( \kappa_I = 2.5 \). This is the value estimated by Christiano et al. (2005). We require that capital utilization \( u_t = 1 \) in steady state, assume that the cost of utilization function \( A_1 = 0 \) and set \( \sigma_a = A_1''(1)/A_1'(1) = 0.01 \). Again, this is the value estimated by Christiano et al. (2005).
References


<table>
<thead>
<tr>
<th>States Most Sensitive to Aggregate Military Buildups</th>
</tr>
</thead>
<tbody>
<tr>
<td>Missouri</td>
</tr>
<tr>
<td>Connecticut</td>
</tr>
<tr>
<td>Texas</td>
</tr>
<tr>
<td>Vermont</td>
</tr>
<tr>
<td>New Hampshire</td>
</tr>
<tr>
<td>Massachusetts</td>
</tr>
<tr>
<td>Kansas</td>
</tr>
<tr>
<td>California</td>
</tr>
<tr>
<td>Georgia</td>
</tr>
<tr>
<td>Louisiana</td>
</tr>
</tbody>
</table>

The table lists the 10 states for which log state military procurement spending increases the most when log national military procurement spending increases in descending order.
### TABLE II
The Effects of Military Spending

<table>
<thead>
<tr>
<th>Prime Military Contracts</th>
<th>Output</th>
<th>Output defl. State CPI</th>
<th>Employment</th>
<th>CPI</th>
<th>Population</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>States</td>
<td>Regions</td>
<td>States</td>
<td>Regions</td>
<td>States</td>
</tr>
<tr>
<td></td>
<td>1.43</td>
<td>1.85</td>
<td>1.34</td>
<td>1.85</td>
<td>1.28</td>
</tr>
<tr>
<td></td>
<td>(0.36)</td>
<td>(0.58)</td>
<td>(0.36)</td>
<td>(0.71)</td>
<td>(0.29)</td>
</tr>
<tr>
<td>Prime Contracts plus</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Military Compensation</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1.62</td>
<td>1.62</td>
<td>1.36</td>
<td>1.44</td>
<td>1.39</td>
</tr>
<tr>
<td></td>
<td>(0.40)</td>
<td>(0.84)</td>
<td>(0.39)</td>
<td>(0.96)</td>
<td>(0.32)</td>
</tr>
</tbody>
</table>

Each cell in the table reports results for a different regression with a shorthand for the main regressor of interest listed in the far left column. A shorthand for the dependent variable is stated at the top of each column. The dependent variable is a two year change divided by the initial value in each case. Output and employment are per capita. The regressor is the two year change divided by output. Military spending variables are per capita except in Population regression. Standard errors are in parentheses. All regressions include region and time fixed effects, and are estimated by two stage least squares. The sample period is 1966-2006 for output, employment and population, and 1969-2006 for the CPI. Output is state GDP, first deflated by the national CPI and then by our state CPI measures. Employment is from the BLS payroll survey. The CPI measure is described in the text. Standard errors are clustered by state or region.
### TABLE III
Alternative Specifications for Effects of Military Spending

<table>
<thead>
<tr>
<th></th>
<th>1. Output Level Instr.</th>
<th>2. Employment Level Instr.</th>
<th>3. Output per Working Age</th>
<th>4. Output OLS</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>States</td>
<td>Regions</td>
<td>States</td>
<td>Regions</td>
</tr>
<tr>
<td>Prime Military Contracts</td>
<td>2.48</td>
<td>2.75</td>
<td>1.81</td>
<td>2.51</td>
</tr>
<tr>
<td></td>
<td>(0.94)</td>
<td>(0.69)</td>
<td>(0.41)</td>
<td>(0.31)</td>
</tr>
<tr>
<td>Prime Contracts plus Military Comp.</td>
<td>4.79</td>
<td>2.60</td>
<td>2.07</td>
<td>1.97</td>
</tr>
<tr>
<td></td>
<td>(2.65)</td>
<td>(1.18)</td>
<td>(0.67)</td>
<td>(0.98)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>5. Output w/ Oil Controls</th>
<th>6. Output w/ Real Int. Contr.</th>
<th>7. Output LIML</th>
<th>8. BEA Employment</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>States</td>
<td>Regions</td>
<td>States</td>
<td>Regions</td>
</tr>
<tr>
<td>Prime Military Contracts</td>
<td>1.32</td>
<td>1.89</td>
<td>1.40</td>
<td>1.80</td>
</tr>
<tr>
<td></td>
<td>(0.36)</td>
<td>(0.54)</td>
<td>(0.35)</td>
<td>(0.59)</td>
</tr>
<tr>
<td>Prime Contracts plus Military Comp.</td>
<td>1.43</td>
<td>1.72</td>
<td>1.61</td>
<td>1.59</td>
</tr>
<tr>
<td></td>
<td>(0.39)</td>
<td>(0.66)</td>
<td>(0.40)</td>
<td>(0.84)</td>
</tr>
</tbody>
</table>

Each cell in the table reports results for a different regression with a shorthand for the main regressor of interest listed in the far left column. A shorthand for the dependent variable plus some extra description is stated at the top of each column. The main regressor is the two year change divided by output. Standard errors are in parentheses. Specifications: 1) and 2) Use national military spending scaled by fraction of military spending in the state in 1966-1971 relative to the average fraction as the instrument for state spending; 3) Constructs per-capita output using the working age population, which is available starting in 1970; 4) OLS estimates of the benchmark specification; 5) Adds the price of oil interacted with state dummies as controls; 6) Adds the real interest rate interacted with state dummies as controls; 7) LIML estimate of baseline specification; 8) Estimates the employment regression using the BEA employment series, which starts in 1969. All specifications include time and regions fixed effects in addition to the main regressor of interest. Standard errors are clustered by state or region depending on the specification.
<table>
<thead>
<tr>
<th>Sector</th>
<th>Weight</th>
<th>States</th>
<th>Regions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Construction</td>
<td>0.05</td>
<td>5.43*</td>
<td>5.51*</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(1.24)</td>
<td>(1.33)</td>
</tr>
<tr>
<td>Manufacturing</td>
<td>0.20</td>
<td>2.83*</td>
<td>3.45*</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.95)</td>
<td>(1.50)</td>
</tr>
<tr>
<td>Retail</td>
<td>0.09</td>
<td>1.36*</td>
<td>1.78*</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.28)</td>
<td>(0.51)</td>
</tr>
<tr>
<td>Services</td>
<td>0.18</td>
<td>0.99*</td>
<td>0.84*</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.39)</td>
<td>(0.41)</td>
</tr>
<tr>
<td>Wholesale</td>
<td>0.07</td>
<td>0.44</td>
<td>0.80</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.35)</td>
<td>(0.63)</td>
</tr>
<tr>
<td>Mining</td>
<td>0.02</td>
<td>-0.48</td>
<td>12.88</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(3.03)</td>
<td>(6.90)</td>
</tr>
<tr>
<td>Agriculture</td>
<td>0.02</td>
<td>1.85</td>
<td>0.72</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(1.13)</td>
<td>(3.81)</td>
</tr>
<tr>
<td>Transportation and Utilities</td>
<td>0.08</td>
<td>-0.05</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.41)</td>
<td>(0.68)</td>
</tr>
<tr>
<td>Finance, insurance, rental, estate</td>
<td>0.17</td>
<td>0.22</td>
<td>1.93</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.71)</td>
<td>(1.39)</td>
</tr>
<tr>
<td>Government</td>
<td>0.13</td>
<td>0.15</td>
<td>0.30</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.34)</td>
<td>(0.64)</td>
</tr>
<tr>
<td>Federal Military</td>
<td>0.01</td>
<td>0.23</td>
<td>-1.37</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(0.82)</td>
<td>(1.87)</td>
</tr>
</tbody>
</table>

The table reports results of regressions of the two year change sectoral state output on the two year change in state military spending. All regressions include region and time fixed effects, and are estimated by two stage least squares. The sample period is 1966-2006. The first data column reports the weight of each sector in total output over our sample period. All variables are in per capita terms. A star indicates statistical significance at the 5% level.
### TABLE V
Effects of Military Spending in High Versus Low Unemployment Periods

<table>
<thead>
<tr>
<th></th>
<th>Output National Slack</th>
<th>Output State Slack</th>
<th>Employment National Slack</th>
<th>Employment State Slack</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta_h$</td>
<td>3.54</td>
<td>4.31</td>
<td>1.85</td>
<td>1.32</td>
</tr>
<tr>
<td></td>
<td>(1.55)</td>
<td>(1.80)</td>
<td>(0.87)</td>
<td>(0.81)</td>
</tr>
<tr>
<td>$\beta_l - \beta_h$</td>
<td>-2.80</td>
<td>-3.37</td>
<td>-0.75</td>
<td>0.03</td>
</tr>
<tr>
<td></td>
<td>(1.49)</td>
<td>(1.84)</td>
<td>(0.89)</td>
<td>(0.84)</td>
</tr>
</tbody>
</table>

A shorthand for the dependent variable is stated at the top of each column. The dependent variable is a two year change divided by the initial value in each case. All variables are per capita. Standard errors are in parentheses. The unit of observation is U.S. states for all regressions in the table. The two regressors are 1) the two year change in military spending and 2) the two year change in military spending interacted with a dummy indicating low slackness. We employ two different measures of slackness: "National Slack" refers to whether the national unemployment rate is below its median value over the sample period; "State Slack" refers to whether the state unemployment rate is below its median value over the sample period. This yields the effect of spending during high unemployment periods ($\beta_h$) and the difference between the effect of spending during low and high unemployment periods ($\beta_l - \beta_h$). The National Slack regressions include state and time fixed effects. The State Slack regressions include state and time fixed effects interacted with the low slackness dummy. The regression are estimated by two stage least squares. The sample period is 1966-2006. Output is state GDP. Employment is from the BLS payroll survey.

### TABLE VI
Government Spending Multiplier in Separable Preferences Model

<table>
<thead>
<tr>
<th></th>
<th>Closed Economy</th>
<th>Open Economy</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Agg. Multiplier</td>
<td>Rel. Multiplier</td>
</tr>
<tr>
<td><strong>Panel A: Sticky Prices</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Volcker-Greenspan Monetary Policy</td>
<td>0.20</td>
<td>0.83</td>
</tr>
<tr>
<td>Constant Real Rate</td>
<td>1.00</td>
<td>0.83</td>
</tr>
<tr>
<td>Constant Nominal Rate</td>
<td>$\infty$</td>
<td>0.83</td>
</tr>
<tr>
<td>Constant Nominal Rate ($\rho_g=0.85$)</td>
<td>1.70</td>
<td>0.90</td>
</tr>
<tr>
<td><strong>Panel B: Flexible Prices</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Constant Income Tax Rates</td>
<td>0.39</td>
<td>0.43</td>
</tr>
<tr>
<td>Balanced Budget</td>
<td>0.32</td>
<td>0.43</td>
</tr>
</tbody>
</table>

The table reports the government spending multiplier for output deflated by the regional CPI for the model presented in the text with the separable preferences specification. Panel A presents results for the model with sticky prices, while panel B presents results for the model with flexible prices. The first three rows differ only in the monetary policy being assumed. The fourth row varies the persistence of the government spending shock relative to the baseline parameter values. The fifth and sixth rows differ only in the tax policy being assumed.
### TABLE VII
Government Spending Multiplier in GHH Model

<table>
<thead>
<tr>
<th>Panel A: Sticky Prices</th>
<th>Closed Economy Agg. Multiplier</th>
<th>Open Economy Rel. Multiplier</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volcker-Greenspan Monetary Policy</td>
<td>0.12</td>
<td>1.42</td>
</tr>
<tr>
<td>Constant Real Rate</td>
<td>7.00</td>
<td>1.42</td>
</tr>
<tr>
<td>Constant Nominal Rate</td>
<td>$\infty$</td>
<td>1.42</td>
</tr>
<tr>
<td>Constant Nominal Rate ($\rho_g=0.50$)</td>
<td>8.73</td>
<td>2.04</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Panel B: Flexible Prices</th>
<th>Closed Economy Agg. Multiplier</th>
<th>Open Economy Rel. Multiplier</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant Income Tax Rates</td>
<td>0.00</td>
<td>0.30</td>
</tr>
<tr>
<td>Balanced Budget</td>
<td>-0.18</td>
<td>0.30</td>
</tr>
</tbody>
</table>

The table reports the government spending multiplier for output deflated by the regional CPI for the model presented in the text with the GHH preferences specification. Panel A presents results for the model with sticky prices, while panel B presents results for the model with flexible prices. The first three rows differ only in the monetary policy being assumed. The fourth row varies the persistence of the government spending shock relative to the baseline parameter values. The fifth and sixth rows differ only in the tax policy being assumed.

### TABLE VIII
Government Spending Multipliers in Incomplete Markets Model

<table>
<thead>
<tr>
<th>Panel A: Sticky Prices</th>
<th>Closed Economy Agg. Multiplier</th>
<th>Open Economy Rel. Multiplier</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline Model (Complete Markets)</td>
<td>0.20</td>
<td>0.83</td>
</tr>
<tr>
<td>Incomplete Markets, Locally Financed</td>
<td>0.18</td>
<td>0.84</td>
</tr>
<tr>
<td>Incomplete Markets, Federally Financed</td>
<td>0.18</td>
<td>0.90</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Panel B: Flexible Prices</th>
<th>Closed Economy Agg. Multiplier</th>
<th>Open Economy Rel. Multiplier</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline Model (Complete Markets)</td>
<td>0.39</td>
<td>0.43</td>
</tr>
<tr>
<td>Incomplete Markets, Locally Financed</td>
<td>0.39</td>
<td>0.41</td>
</tr>
<tr>
<td>Incomplete Markets, Federally Financed</td>
<td>0.39</td>
<td>0.40</td>
</tr>
</tbody>
</table>

The table reports the government spending multiplier for output deflated by the regional CPI for a version of the model presented in the text with separable utility in which the only financial asset traded across regions is a non-contingent bond. Panel A presents results for the model with sticky prices, while panel B presents results for the model with flexible prices.
### TABLE IX
Open Economy Relative Multiplier in Models with Variable Capital

<table>
<thead>
<tr>
<th>Model</th>
<th>Output</th>
<th>CPI Inflation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline Model (Fixed Capital)</td>
<td>1.42</td>
<td>0.17</td>
</tr>
<tr>
<td>Firm-Specific Capital Model</td>
<td>1.47</td>
<td>0.15</td>
</tr>
<tr>
<td>Regional Capital Market Model</td>
<td>0.98</td>
<td>0.11</td>
</tr>
<tr>
<td>Firm-Specific Capital Model, Flexible Prices</td>
<td>0.25</td>
<td>0.36</td>
</tr>
</tbody>
</table>

The table reports the open economy relative government spending multiplier for output and CPI inflation for our baseline model with GHH preferences and the two models with variable capital also with GHH preferences. Output is deflated by the regional CPI.
Figure I
Prime Military Contract Spending as a Fraction of State GDP
Figure II
Prime Military Contracts and Military Shipments
FIGURE III
Quantiles of Change in Output Versus Predicted Change in Military Spending
The figure shows averages of changes in output and predicted military spending (based on our first-stage regression), grouped by 30 quantiles of the predicted military spending variable. Both variables are demeaned by year and state fixed effects.
Figure IV
Prices and Real Interest Rates after a Government Spending Shock
The figure plots the relative price level and the relative real interest rate in the two regions for the model with separable preferences after a positive government spending shock to the home region.

Figure V
Consumption and Real Interest Rate after a Government Spending Shock
The figure plots the relative consumption and the relative real interest rate in the two regions for the model with separable preferences after a positive government spending shock to the home region.
Output and Consumption after a Government Spending Shock in GHH Model

The figure plots the relative output and consumption in the two regions for the model with GHH preferences after a positive government spending shock to the home region.